



**UNIVERSITY OF SWAZILAND
MAIN EXAMINATION PAPER**

PROGRAMMES:

BSc. ABE 3,

COURSE CODE: ABE 303

TITLE OF PAPER: FLUID AND SOIL MECHANICS

TIME ALLOWED: TWO (2) HOURS

SPECIAL MATERIAL REQUIRED: NONE

**INSTRUCTIONS: ANSWER QUESTION ONE AND ANY TWO OTHER
QUESTIONS**

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THE CHIEF INVIGILATOR**

QUESTION 1

- a. Water is flowing over a sharp-crested rectangular weir of width 35cm into a cylindrical tank of diameter 75 cm. In 20 seconds the depth of water in the tank rises 1.2m. Assuming a discharge coefficient of 0.9, determine the height of the water above the weir in mm. **[10 marks]**
- b. Soil from a borrow pit is to be used for a constructed fill in the construction of a storage lagoon. The construction details call for the fill to be placed and compacted to 95% Proctor density. The material to be used for the fill comes from a borrow pit with a void ratio of 0.60.
- (i) Describe what '95% Proctor density' means. **[5 marks]**
- (ii) What volume of material from the borrow pit will need to be removed to make up the required 1000 m³ of in-place material? **[10 marks]**
- (iii) Plot the relationship between water content and bulk density for a soil undergoing a standard compaction effort. **[5 marks]**
- (iv) Show on the same graph as used for (iii), the effects of increasing or decreasing the compaction effort. **[5 marks]**
- (v) Suggest ways that the required compaction might be achieved in the construction. **[5 marks]**

QUESTION 2

- a. A retaining wall 5 m high supports a backfill consisting of 2 m of sandy clay overlying 3m of sand. The gravimetric water level water level coincides with the upper surface of the sand. Given that the soil constants are;

Sandy clay**sand**

$$\rho = 1840 \text{ kg / m}^3$$

$$\rho = 1930 \text{ kg / m}^3$$

$$c = 11.5 \text{ kN / m}^2$$

$$c = 0 \text{ kN / m}^2$$

$$\phi = 10^\circ$$

$$\phi = 35^\circ$$

- (i) Determine the total active thrust on the retaining wall and its point of action, assuming tension cracks have developed. **[10 marks]**
- (ii) If it were possible to lower the water level by 2m, without altering the soil properties, what then would be the active thrust on the wall? Again, assume tension cracks would develop. **[10 marks]**
- b. Explain why the velocity measured by the Pitot-static tube is higher than that measured by the venturimeter? **[10 marks]**

QUESTION 3

- a. Derive an expression for the bulk density of a partially saturated soil in terms of specific gravity of the particle, G_s , the void ratio, e , the degree of saturation, S_r , and the density of water, ρ_w . **[10 marks]**
- b. Starting with the Bernoulli and Continuity equations derive the following expression that can be used to measure flow rate with a venturi meter. **[10 marks]**

$$Q_{actual} = c_d A_1 A_2 \sqrt{\frac{2g \left[\frac{P_1 - P_2}{\rho g} + z_1 - z_2 \right]}{A_1^2 - A_2^2}}$$

- c. Show that when the pressure difference is measured using a manometer the following expression can be used; **[10 marks]**

$$Q_{actual} = c_d A_1 A_2 \sqrt{\frac{2gh \left(\frac{\rho_{man}}{\rho} - 1 \right)}{A_1^2 - A_2^2}}$$

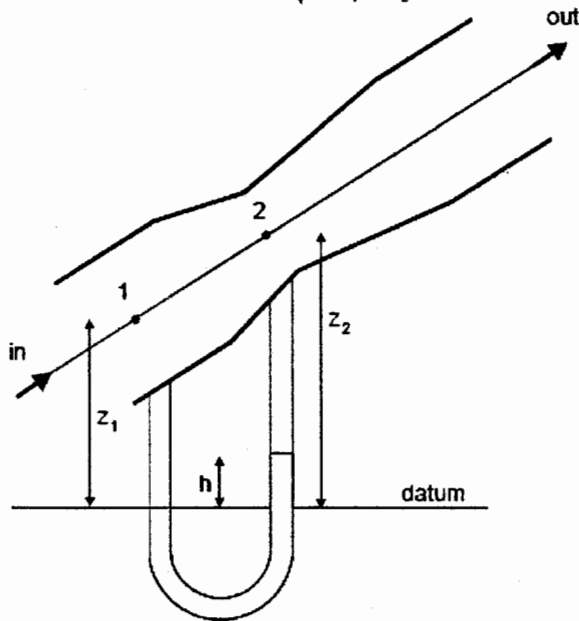
QUESTION 4

a. A concrete-lined trapezoidal channel with uniform flow has a normal depth a normal depth of 2 m. The base width is 5 m and the side slopes are equal at 1:2.

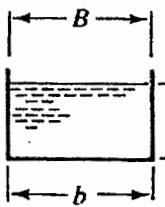
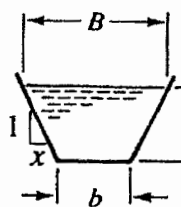
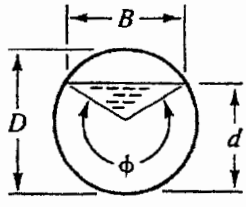
Taking Manning's $n = 0.015$ and the bed slope $S = 0.001$, and viscosity $\mu = 1.14 \times 10^{-3} \text{ N s/m}^2$, calculate;

- (i) Discharge [5marks]
- (ii) Mean velocity [5marks]
- (iii) Reynolds number [5marks]

b. A venturimeter (see figure) is used to measure the flow of water in a pipe of diameter 100mm. The throat diameter (2) of the venturimeter is 60mm and it has a coefficient of discharge of 0.9. When a flow of 100 litres/second is flowing the attached manometer shows a head difference of 60cm, what is the density of the manometric fluid of the manometer? [15marks]



APPENDIX

	 Rectangle	 Trapezoid	 Circle
area, A	by	$(b + xy)y$	$\frac{1}{8}(\phi - \sin \phi)D^2$
wetted perimeter, P	$b + 2y$	$b + 2y\sqrt{1 + x^2}$	$\frac{1}{2}\phi D$
top width, B	b	$b + 2xy$	$\left(\sin \frac{\phi}{2}\right)D$
hydraulic radius, R	$\frac{by}{b + 2y}$	$\frac{(b + xy)y}{b + 2y\sqrt{1 + x^2}}$	$\frac{1}{4}\left(1 - \frac{\sin \phi}{\phi}\right)D$
hydraulic mean depth, D_m	y	$\frac{(b + xy)y}{b + 2xy}$	$\frac{1}{8}\left(\frac{\phi - \sin \phi}{\sin(1/2\phi)}\right)D$

$$p_a = k_a \gamma z$$

$$p_a = k_a \gamma z - 2c \sqrt{k_a}$$

$$p_a = \gamma z \frac{1}{N_\phi} - 2c \frac{\sqrt{N_\phi}}{N_\phi}$$

$$k_a = \frac{1 - \sin \phi}{1 + \sin \phi} = \tan^2 \left(45 - \frac{\phi}{2} \right)$$

$$p_a = k_a \gamma z$$