#### UNIVERSITY OF SWAZILAND

# FACULTY OF SCIENCE

#### DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING

MAIN EXAMINATION 2010

TITLE OF PAPER: ELECTRONIC MATERIALS & DEVICES II

**COURSE NUMBER: E 450** 

TIME ALLOWED: THREE HOURS

# **INSTRUCTIONS TO CANDIDATES:**

USEFUL DATA AND FORMULAE ARE IN THE APPENDIX.

ANSWER ANY FOUR QUESTIONS . ALL QUESTIONS CARRY EQUAL MARKS

THIS PAPER IS NOT TO BE OPENED UNTIL PERMISSION HAS BEEN GIVEN BY THE INVIGILATOR.

# Question One.

- (a) (i) Draw a sketch of the current voltage characteristics of an n-channel JFET for different values of the gate voltage. (3 marks)
  - (ii) Explain the main features of the current voltage characteristic for the case in which no gate voltage is applied. (4 marks)
  - (iii) State two reasons why a FET is preferred to a BJT.

(2 marks)

(b) The drain current of a JFET is given as

$$I_D = G_0 \left\{ V_D - \frac{2}{3} V_P \left[ \left( \frac{V_i - V_G + V_D}{V_P} \right)^{3/2} - \left( \frac{V_i - V_G}{V_P} \right)^{3/2} \right] \right\} \,,$$

where the symbols have their usual meanings.

(i) Show that in the linear region, the above expression becomes

$$I_D = G_0 \left[ 1 - \left( \frac{V_i - V_g}{V_p} \right)^{1/2} \right] V_D \ . \label{eq:ID}$$

[Hint: expand the term containing V<sub>D</sub> using binomial series]

(6 marks)

- (ii) Define the *threshold voltage*  $V_{th}$  of a JFET and show that it is equal  $V_i V_p$  (5 marks)
- (iii) Define *transconductance* of a JFET and obtain an expression for it. (5 marks)

# **Question Two**

- (a) (i) Explain what is meant by Base-width modulation in a transistor. (3 marks)
  - (ii) Discuss the effects of base- width modulation in the performance of a real p-n-p transistor in normal operation.

(5 marks)

- (b) The punch through voltage of a germanium p-n-p transistor is 25V. The base doping is  $10^{15}$  cm<sup>-3</sup>. The emitter and collector dopant concentrations are  $10^{19}$  cm<sup>-3</sup> each. Calculate
  - (i) the built-in voltage,

(3 marks)

(ii) the zero bias base width,

(4 marks)

(iii) the common emitter current gain  $\beta$ , and

- (8 marks)

(iv) the common base current gain  $\alpha$  for a reverse bias of 10 V across the collector-base junction. (2 marks)

Assume  $\tau_B = 10^{-6}$ s,  $n_i$  for  $Ge = 2.4 \times 10^{13}$  cm<sup>-3</sup>, T = 300 K

[25]

#### **Question Three**

(a) A small signal ac voltage is superimposed on the dc bias of a p-n-p diffusion transistor in the normal operation. Neglecting the depletion region charges show that the small signal common base current gain of the transistor can be written as

$$\alpha(\omega) = \frac{\alpha_0}{1 + \frac{j\omega}{\omega_\alpha}}$$

where symbols have their usual meanings.

(9 marks)

Given:

$$i_E = (Q_N + q_N)(\frac{1}{\tau_N} + \frac{1}{\tau_{RN}}) + \frac{d}{dt}(Q_N + q_N); i_C = -\frac{Q_N + q_N}{\tau_N}$$

Hint: assume that the charge associated with the ac voltage is of the form  $q_N = q_{N0} \exp(j\omega t)$ 

(b) Given that the beta cut - off frequency  $f_{\beta} = f_{\alpha} (1 - \alpha_{o})$ , show that the common emitter current gain can be expressed as:

$$\beta(\omega) = \frac{\beta_0}{1 + \frac{jf}{f_\beta}} \tag{7 marks}$$

(c) A transistor operating at 20 MHz has current gain  $\beta = 20$ . Neglecting junction capacitance and series resistance, calculate:

(i)	the beta cut-off frequency f <sub>β</sub>	(4 marks)
(ii)	the alpha cut - off frequency $f_{\alpha}$	(3 marks)

(iii) the gain bandwidth frequency  $f_T$  (2 marks)

[Given that  $\beta_0 = 100$ ] [25]

# **Question Four.**

- (a) (i) Give details of the Float-Zone method in the fabrication of single crystal silicon wafer with the help of a schematic diagram of the set up.
  - (ii) State the advantages of Float-zone technique over the Czochralski method of wafer preparation.

(10 marks)

(iii) What is zone refining? Explain.

(4 marks)

(iv) Explain the process of neutron transmutation doping mentioning its importance. (4 marks)

(b) A silicon crystal doped with phosphorus is pulled from its melt. Calculate how many grams of phosphorus should be added to 1 kg of silicon to get a donor concentration of 10<sup>16</sup> cm<sup>-3</sup> during the initial growth. The distribution coefficient of phosphorus is 0.35. Atomic weight of phosphorus is 30.97, density of silicon is 2.53 g cm<sup>-3</sup>.

(7 marks)

[25]

#### **Question Five**

(a) A, B, C, and D are four points on the periphery of an odd- shaped semiconductor sample of thickness 0.2 mm. Following are the results obtained in the van der Paw method for resistivity measurements on the sample.

$$V_{Dc} = 5V$$
,  $V_{Bc} = 10V$ ,  $I_{AB} = 50$  mA,  $I_{AD} = 200$  mA.

Calculate the resistivity and sheet resistance of the sample.

(8 marks)

(b) The hole mobility of the sample in question (a) above is 400 cm<sup>2</sup>/Vs. Determine the Hall voltage V<sub>BD</sub> developed across the points B and D of the sample when it is placed in a magnetic field of 5x10<sup>-5</sup> Wb cm<sup>-2</sup> and 5 mA current is passed across A and C.

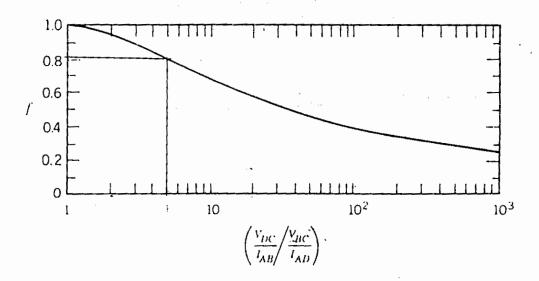
(7 marks)

(c) In a Haynes- Shockley experiment the following data were obtained in a semiconductor sample of length 2 cm.

$$x_o = 1 \text{ cm}$$
  
 $V_1 = 10V$   
 $t_o = 200 \text{ } \mu\text{s}$   
 $\Delta t = 30 \text{ } \mu\text{s}$ 

- (i) Calculate the mobility and the diffusion coefficient of the minority carriers.
- (ii) Verify whether or not your results agree with Einstein's relation.
  (T=300K) (10 marks)

# APPENDIX A



Correction factor for van der Pauw arrangement.

# APPENDIX B PHYSICAL CONSTANTS

Quantity	Symbol	Value
Angstrom unit	Å	$1 \text{ Å} = 10^{-8} \text{ cm} = 10^{-10} \text{ m}$
Avogadro number	N	$6.023 \times 10^{23}$ /mol
Boltzmann constant	k	$8.620 \times 10^{-5} \text{ eV/K} = 1.381 \times 10^{-23} \text{ J/K}$
Electronic charge	q	$1.602 \times 10^{-19} \mathrm{C}$
Electron rest mass	$m_{\nu}$	$9.109 \times 10^{-31} \text{ kg}$
Electron volt	eV	$1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$
Gas constant	R	1.987 cal/mole-K
Permeability of free space	$\mu_o$	$1.257 \times 10^{-6}  \text{H/m}$
Permittivity of free space	$\varepsilon_{a}$	$8.850 \times 10^{-12} \text{ F/m}$
Planck constant	h	6.626 × 10 <sup>-14</sup> J-s
Proton rest mass	$m_p$	$1.673 \times 10^{-27} \text{ kg}$
1ι/2π	h	$1.054 \times 10^{-M} \text{ J-s}$
Thermal voltage at 300 K	$\nu_r$	0.02586 V
Velocity of light in vacuum	c ·	2.998 × 10 <sup>10</sup> cm/s
Wavelength of 1-cV quantum	λ	1.24 μm

TABLE 4.2 APPEX
Properties of Ge, Si and GaAs at 300 K

Property	Ge	Si	GaAs
Atomic/molecular weight	72.6	28.09	144.63
Density (g cm <sup>-3</sup> )	5.33	2.33	5.32
Dielectric constant	16.0	11.9	13.1
Effective density of states		•	•
Conduction band, N <sub>C</sub> (cm <sup>-3</sup> )	$1.04 \times 10^{19}$	$2.8 \times 10^{19}$	$4.7 \times 10^{17}$
Valence band $N_{\nu}$ (cm <sup>-3</sup> )	$6.0 \times 10^{18}$	$1.02 \times 10^{19}$	$7.0 \times 10^{18}$
Electron affinity (eV)	4.01	4.05	4.07
Energy gap, $E_s$ (eV)	0.67	1.12	1.43
Intrinsic carrier			
concentration, $n_i$ (cm <sup>-3</sup> )	$2.4 \times 10^{13}$	$1.5 \times 10^{10}$	$1.79 \times 10^{6}$
Lattice constant (Å)	5.65	5.43	5.65
Effective mass			
Density of states $m_e^*/m_o$	0.55	1.18	0.068
$m_h^*/m_o$	0.3	0.81	0.56
Conductivity $m_e/m_o$	0.12	0.26	0.09
$m_h/m_o$	0.23	0.38	
Melting point (°C)	937	1415	1238
Intrinsic mobility		•	
Electron (cm <sup>2</sup> V <sup>-1</sup> sec <sup>-1</sup> ) , N ~	3900	1350	8500
Hole (cm <sup>2</sup> V <sup>-1</sup> sec <sup>-1</sup> ) $\mathcal{N}_r$	1900	480	400

#### APPENDIX A

Some useful equations.

$$I_D = G_0 \left\{ V_D - \frac{2}{3} V_P \left[ \left( \frac{V_i - V_G + V_D}{V_P} \right)^{3/2} - \left( \frac{V_i - V_G}{V_P} \right)^{3/2} \right] \right\}$$

$$f_{\text{max}} = \left[ \frac{f_T}{8\pi r_B C_c} \right]^{1/2}$$

$$W_B = W_{B0} - \left[ \frac{2\varepsilon_S}{qN_d} (V_i - V_{CB}) \right]^{1/2}$$

$$\omega_{\alpha} = \frac{2.43D_{B}}{\omega_{B}^{2}} \left[ 1 + \left( \frac{\eta}{2} \right)^{4/3} \right]$$

$$\frac{I_{NE}}{I_{PE}} = \frac{N_D D_E L_B \tanh(W_B / L_B)}{N_a D_B L_E \tanh(W_E / L_E)}$$

$$\alpha(\omega) = \frac{\alpha_0}{1 + j\omega/\omega_{\alpha}} \exp\left(-j\frac{m\omega}{\omega_{\alpha}}\right)$$

$$G_E \approx \frac{N_a L_E}{D_E}$$

$$\rho = \frac{\pi d}{2\ln 2} \left( \frac{V_{DC}}{I_{AB}} + \frac{V_{BC}}{I_{AD}} \right) f$$