# UNIVERSITY OF SWAZILAND MAIN EXAMINATION, SECOND SEMESTER MAY 2011 FACULTY OF SCIENCE

## DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING

TITLE OF PAPER:

FUNDAMENTALS OF POWER ENGINEERING

COURSE CODE:

EE351

TIME ALLOWED:

THREE HOURS

C 1: 1-4)	Eii No	
Candidates	Examination Number	

#### **INSTRUCTIONS:**

- 1. Write your Examination number in the space provided above.
- 2. Answer all questions. Marks for different questions are indicated at the beginning of each question.
- 3. Write your answers in the space provided on the question paper. If you need more space to complete your answer you may use the space at the back of the question paper or you may use the examination Answer Book. In either case you must mention where using "continued at the back" or "continued in the Answer Book".
- 4. At the end of the Examination put the question paper inside your Answer Book and submit both.
- 5. Rough work may be done in the answer Book and crossed through.

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HAS BEEN GIVEN BY THE INVIGILATOR
THIS PAPER CONTAINS SIXTEEN (16) PAGES

#### Question 1: Solve the following questions (30 marks):

1-The magnetic field intensity H is 110 AT/m, the core mean path length  $l_c = 0.4$  m, what is current in the coil of N=200 turns?

- 2- The magnetic core mean path length  $l_c = 1.5$  m, the core cross section area A=0.2  $m^2$ , the relative permeability of the core material  $\mu_r = 2000$ , and the relative permeability of the air  $\mu_0 = 4\pi * 10^{-7}$ . Calculate the reluctance R of the core. R=
- 3- A magnetic core has reluctance R= 16000 At/Wb, and has 200 turns coil wrapped around the core. How much flux is produced when a 3 A current flows in the coil?
- 4- What is the magnitude and direction of induced force on a conductor of a length l= 3 m, carrying a current i=2.5 A from up to down and present in uniform magnetic field density B=0.8 T point to page?

Direction of F =

5- What is the magnitude of induced voltage on a conductor moving with a velocity v=15 m/sec in uniform magnetic field density B=0.6T point to page, the wire length l=2 m?

$$E_{ind} =$$

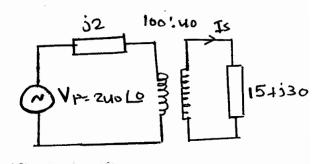
6-In 5 before, mention the direction of the induced voltage, magnetic field density and velocity according to the fingers of the right hand. Index point to:

Middle point to:

Thump point to:

7- A single phase transformer, has the number of turns in primary  $N_{p}$ =100 turns, number of turn in secondary  $N_s$  =40 turns, the primary source voltage  $V_p = 240 \angle 0$ with source impedance = j2 ohm, and a load impedance in secondary= 15+j30 ohm. Calculate the transformer turns ratio, the primary and secondary currents, the load voltage and the complex, active and reactive power drawn at the load.

(Calculate: a,  $I_p$ ,  $I_s$ ,  $V_{load}$ ,  $S_{load}$ ,  $P_{load}$ ,  $Q_{load}$ )



8- In three phase connected transformer, each of the three transformers has number of turns in primary  $N_p=200$  and number of turns in secondary  $N_s=400$ , what will be the ratio between the line to line voltage at the primary to the line to line voltage at the secondary in case of

a) Y - Y Connected transformer.

$$\frac{V_{Lp}}{V_{LS}} =$$

b)  $Y - \Delta$  Connected transformer.

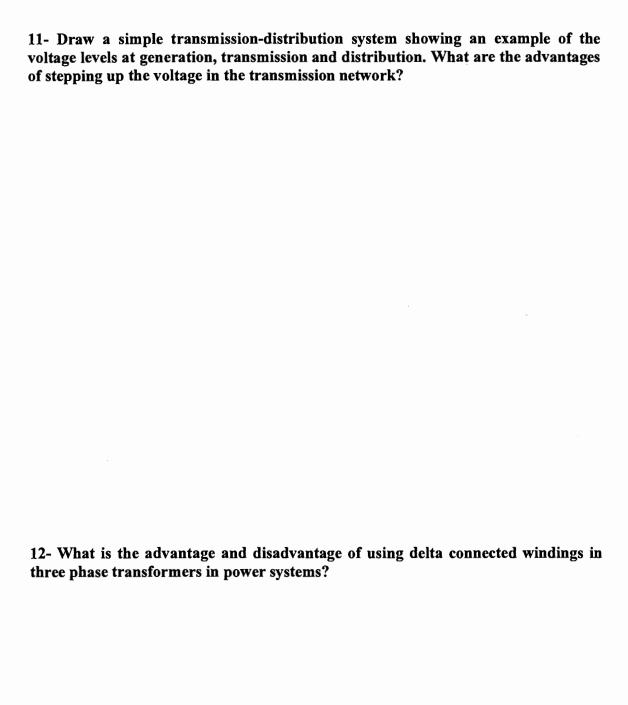
$$\frac{V_{Lp}}{V_{LS}} =$$

c)  $\Delta - Y$  Connected transformer.

$$\frac{V_{Lp}}{V_{LS}} =$$

9- Three phase  $\Delta - Y$  connected transformer bank steps up the generator voltage from 11 KV (line to line) to 220 KV (line to line). Calculate the primary phase voltage, the secondary phase voltage and the transformer turns ratio. (Calculate:  $V_P$ ,  $V_S$ , a)

10- List three methods that can be used to increase the voltage level in power systems when an under voltage is detected in the system.



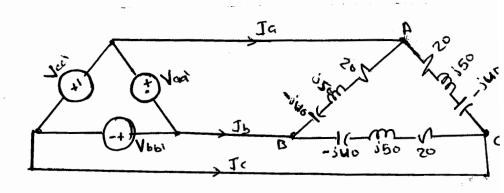
### Question 2: In the following (17 marks):

In the following  $\Delta - \Delta$  connection between sources and loads if

$$\begin{split} V_{aa'} &= 200 \angle 0^{\circ} \qquad V \\ V_{bb'} &= 200 \angle -120^{\circ} \qquad V \\ V_{cc'} &= 200 \angle 120^{\circ} \qquad V \\ Z_{\Delta} &= 20 + j50 - j40 \qquad \Omega \end{split}$$

Calculate:

1) The current in each load branch  $I_{\rm AB}$  ,  $I_{\rm BC}$  ,  $I_{\rm CA}$  .



2 ) The line current  $\,I_a\,.\,$ 

3) The total three phase complex, active and reactive power supplied to load. (Calculate:  $S_{3\varphi}$ ,  $P_{3\phi}$ ,  $Q_{3\varphi}$ )

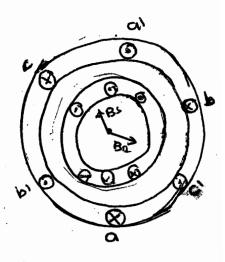
4) The active and reactive power absorbed in the resistor in branch AB. (Calculate:  $P_{\!\scriptscriptstyle R}\,,Q_{\!\scriptscriptstyle R}\,)$ 

5) The active and reactive power absorbed/supplied in the inductor in branch AB. (Calculate:  $P_L\,,Q_L\,)$ 

6) The active and reactive power absorbed/supplied in the capacitor in branch AB. (Calculate:  $P_{C}$  ,  $Q_{C}$  )

Question 3 (16 marks):

1) Explain briefly the principle of operation of three phase induction motor.



2) What is the effect of increasing mechanical load torque on the induction motor?

3) Explain how you can control the induction motor speed.

#### Question 4 (37 marks):

A 480V (line to line voltage), 30 hp, 50 Hz, two poles, Y connected induction motor, has the following impedances in ohms per phase referred to stator circuit.

$$R_1 = 0.8\Omega$$

$$R_2 = 0.5\Omega$$

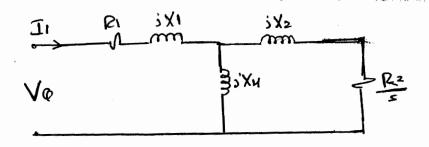
$$X_1 = 1.2\Omega$$

$$X_2 = 0.6\Omega$$

$$X_M = 40\Omega$$

$$s = 0.04$$

The total rotational losses are 1000W. The motor slip is .04 at rated voltage and rated frequency.



1) Calculate the synchronous speed in rpm  $(n_{sync})$  and rad per sec  $(\omega_{sync})$ .

2) Calculate the motor speed in rpm  $(n_m)$  and rad/sec  $(\omega_m)$ .

- 3) Calculate the rotor current frequency  $f_r$ .
- 4) Calculate the total impedance of the circuit  $\,Z_{\mbox{\tiny tot}}\,$  .

5) Calculate the stator phase voltage and current.

$$V_{\varphi} =$$

$$I_1 =$$

6) Calculate the motor power factor.

$$P_f =$$

7) Draw the power flow diagram.

12) Calculate the	power	converted	from	electrical	to	mechanical.

$$P_{conv}$$
 =

13) Calculate the motor output power.

$$P_{out} =$$

14) Calculate the induced torque.

$$T_{ind} =$$

15) Calculate the load torque.

$$T_{load} =$$

16) Calculate the motor efficiency  $\varsigma$  .

8) Calculate the motor input power.

$$P_{in} =$$

9) Calculate the motor stator copper losses.

$$P_{scl} =$$

10) Calculate the air gap power.

$$P_{ag} =$$

11) Calculate the rotor copper losses.

$$P_{rcl} =$$

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20) Given the main equation for  $s_{\rm max}$ , calculate the slip at which the maximum torque occurs and the corresponding speed in rpm.

$$s_{\max} = \frac{R_2}{\sqrt{R_{th}^2 + (X_{th} + X_2)^2}}$$

$$n_{\text{max}} =$$

21) Given the main equation for  $T_{\rm max}$ , calculate the maximum induced torque.

$$T_{\text{max}} = \frac{3V_{th}^{2}}{2\omega_{\text{sym}} \left[ R_{th} + \sqrt{R_{th}^{2} + (X_{th} + X_{2})^{2}} \right]}$$

22) Given the main equation for  $T_{\it start}$  , calculate the starting induced torque.

$$T_{start} = \frac{3V_{th}^{2}R_{2}}{\omega_{syn}[(R_{th} + R_{2})^{2} + (X_{th} + X_{2})^{2}]}$$