

**UNIVERSITY OF SWAZILAND**  
**FACULTY OF SCIENCE**  
**DEPARTMENT OF ELECTRICAL & ELECTRONIC ENGINEERING**  
**FIRST SEMESTER EXAMINATION 2011/12**

**TITLE OF THE PAPER: BASIC ELECTRICAL ENGINEERING**  
**COURSE CODE: EE251**  
**TIME ALLOWED: THREE HOURS**

**INSTRUCTIONS TO CANDIDATES**

1. Answer any **FOUR (4)** questions only.
2. Each question carries 25 marks.
3. Show the steps clearly in all your calculations.
4. State clearly any assumption made.

**DO NOT OPEN THE PAPER UNTIL PERMISSION HAS BEEN  
GRANTED BY THE INVIGILATOR**

**This paper contains EIGHT (8) pages including this page**

## QUESTION 1

(a) Suppose you have seen the readings of 300 kWh at 6 am in a day in your house's pre-paid energy meter connected to the single-phase supply of 230-V supplied by Swaziland Electricity Company (SEC). Between 6 am and 6 pm in the same day you have used the following appliances

- ❖ 120-W Freezer with total off-time of 1 hour during the period
- ❖ 1500-W electric oven for 3 hours
- ❖ 1200-W electric heater for 5 hours
- ❖ 450-W washing machine for 1 hour
- ❖ Three tube lights each of 60-W for 2 hours each

Find the following:

- (i) Expected reading of the pre-paid meter at 6 pm in the same day. [4 marks]
- (ii) The input current from the supply if all the appliances are operated simultaneously when overall power factor is 0.85 (lag). [2 marks]
- (iii) Efficiency of your electrical wiring systems of your house if you find that the actual energy consumption during that period is 0.4 kWh more than that of your expectation. [2 marks]

(b) For the series-parallel network of the Fig. Q1b, find the following

- (i) The current  $I_s$  [6 marks]
- (ii) Find the currents  $I_2$  and  $I_8$  [2 marks]
- (iii) Find the current  $I_7$  [3 marks]
- (iv) Find the voltage  $V_{ab}$  [3 marks]

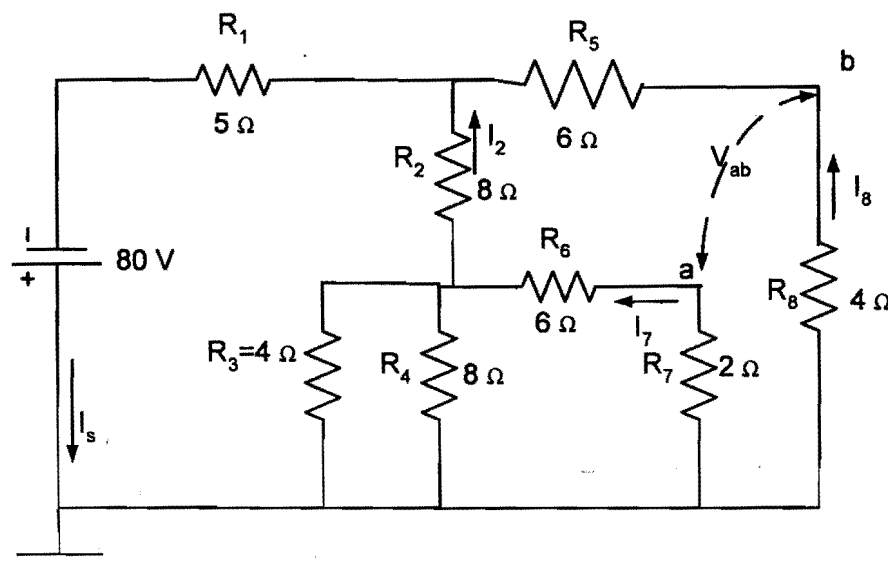


Fig.Q1b

(c) With appropriate diagrams explain the meaning of short and open circuits.

[3 marks]

## QUESTION 2

(a) Find the voltage  $V_s$  across  $R_5$  as shown in Fig.Q2a through applying superposition theorem.

[15 marks]

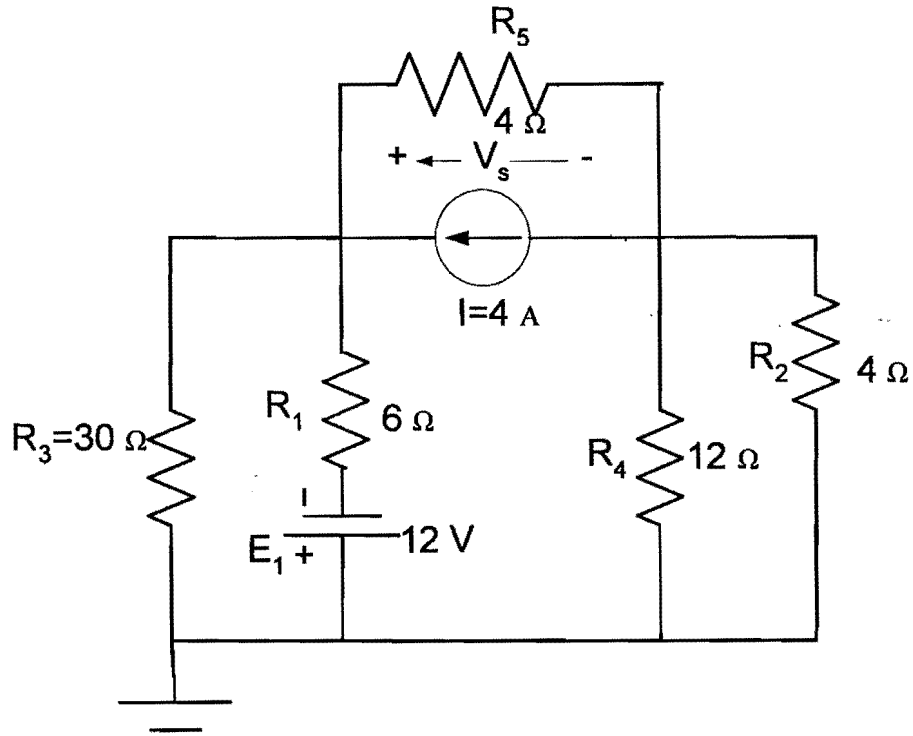


Fig.Q2a

(b) Apply mesh analysis to find the mesh currents for the circuit shown in Fig.Q2b.

Hence, determine the power dissipated in resistor  $R_2$ .

[10 marks]

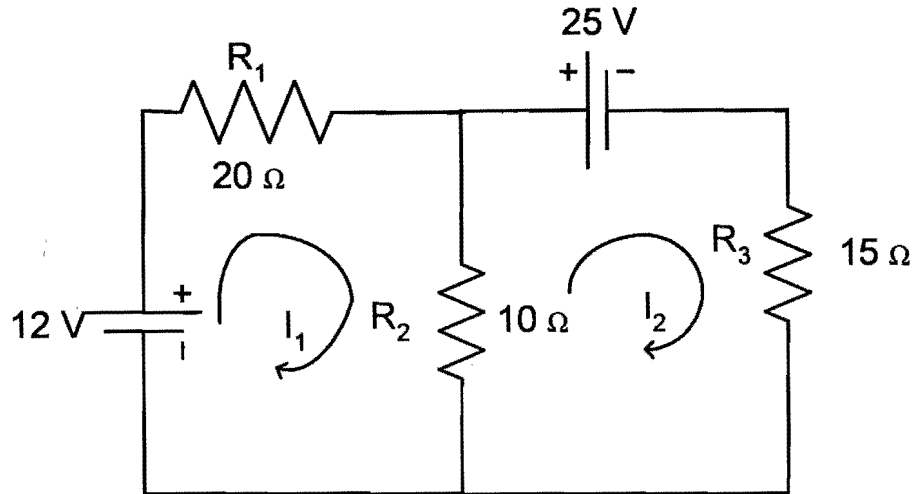


Fig.Q2b

### QUESTION 3

- (a) Using the supernode approach, determine the nodal voltages for the networks of Fig. Q3a below and hence find the current through the DC source of 16V. [11 marks]

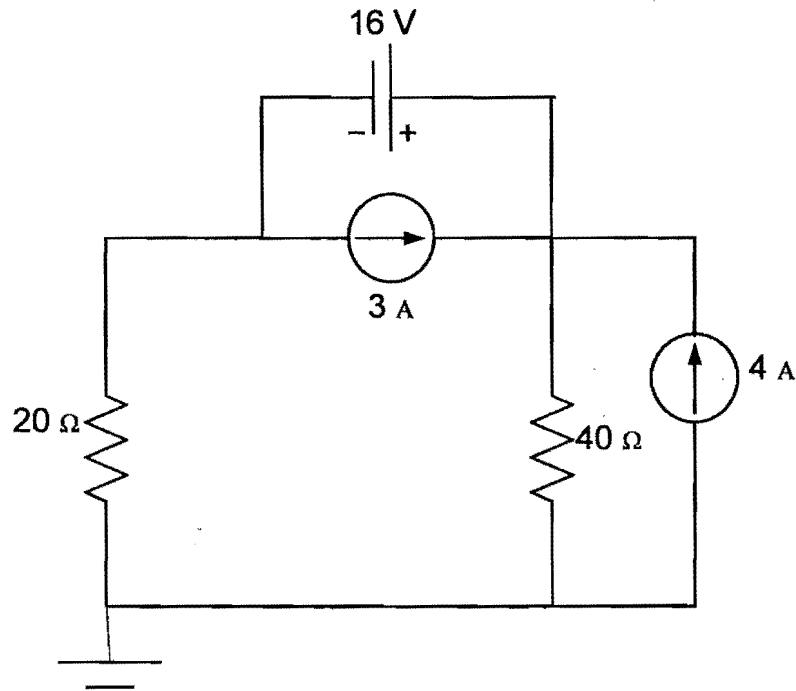


Fig. Q3a

- (b) Find the Thévenin equivalent circuit for the network at the terminals of  $R_L$  of the bridge network of Fig. Q3b below. If maximum power is to be transferred to  $R_L$  what would be its resistance and how much maximum power will be dissipated by  $R_L$ ? [10+4 marks]

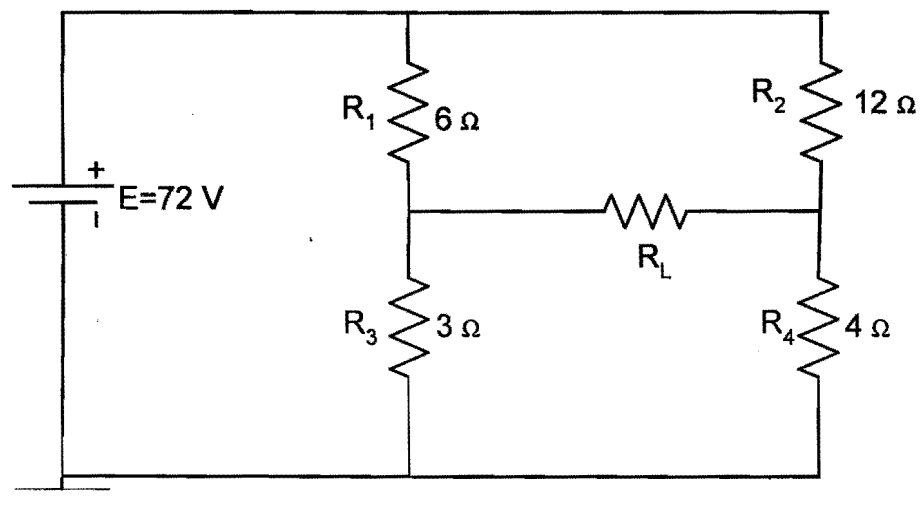


Fig. Q3b

#### QUESTION 4

(a) Given that in the magnetic circuit shown in Fig.Q4a, area (throughout) $=2\times10^{-4}\text{ m}^2$ ,  $l_{ab}=l_{ef}=0.05\text{ m}$ ,  $l_{af}=l_{be}=0.02\text{ m}$ ,  $l_{bc}=l_{de}$ . B-H curve of sheet steel is given in page 8. For air gap  $H_g=(7.96\times10^5)\text{ B}_g\text{ At/m}$

(i) Find the current  $I$  necessary to establish a flux of  $\Phi=2.4\times10^{-4}\text{ Wb}$ . [7 marks]

(ii). Compare the mmf drop across the air gap to that across the rest of the magnetic circuit. Discuss your results using the value of  $\mu$  for each material. [4 marks]

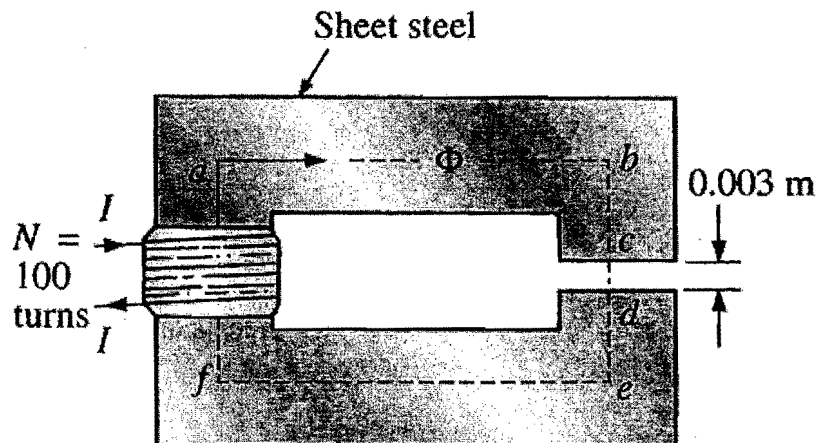


Fig.Q4a

(b) For the circuit shown in Fig.Q4b

(i) Determine the time constant of the circuit .

[2 marks]

(ii) Write the mathematical equation for the voltage  $v_C$  following the closing of the switch.

[2 marks]

(iii) Determine the voltage  $v_C$  after one and five time constants.

[2 marks]

(iv) Write the equations for current  $i_C$  and voltage  $v_R$ .

[3 marks]

(v) Determine the time at which the voltage across the capacitor will be 15 V

[2 marks]

(vi) Sketch the waveforms for  $v_C$  and  $i_C$ .

[3 marks]

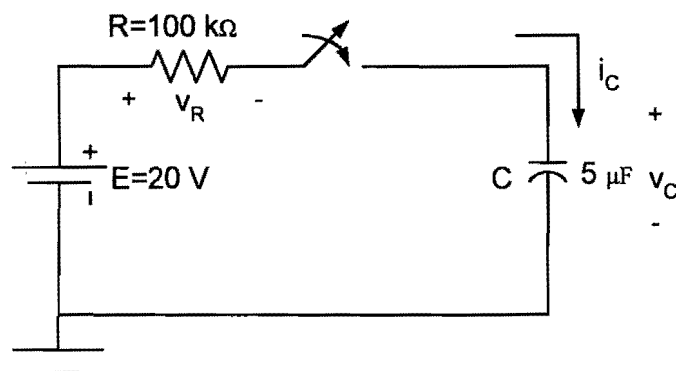


Fig.Q4b

### QUESTION 5

(a) Fig. Q5a below shows the waveform displayed on the screen of an oscilloscope. Note that oscilloscope's vertical sensitivity is 10 mV/div and horizontal sensitivity is 10  $\mu$ s/div. For this waveform,

- (i) Determine the period. [2 marks]
- (ii) Find the frequency. [2 mark]
- (iii) Determine the average value. [4 marks]
- (iv) Determine the rms value. [4 marks]

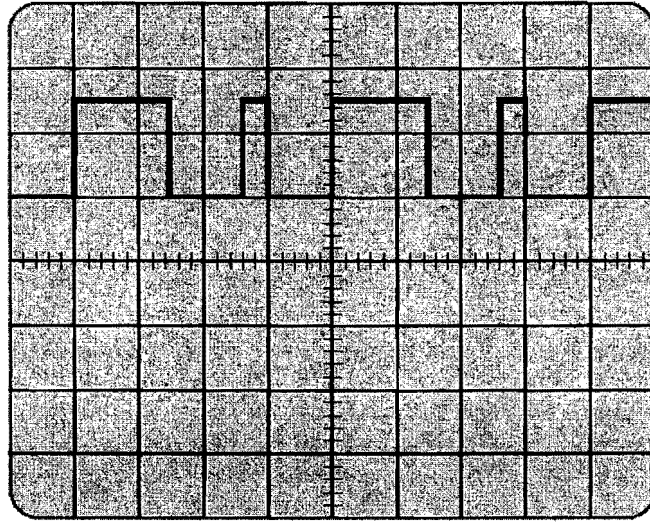


Fig. Q5a

(b) For the circuit shown in Fig.Q5b (next page)

- (i) Determine the magnitude of the current  $I$  at resonance. [1 marks]
- (ii) Find the voltages  $V_R$ ,  $V_L$  and  $V_C$  at resonance, and compare their magnitudes. [4 marks]
- (iii) Determine the quality factor of the circuit. Is it a high or low- $Q$  circuit? [2 marks]
- (iv) If the resonant frequency is 5 kHz, determine the value of  $L$  and  $C$ . [3 marks]
- (v) Find the bandwidth of the response if the resonant frequency is 5 kHz. [1 marks]
- (vi) What are the low and high cutoff frequencies? [2 marks]

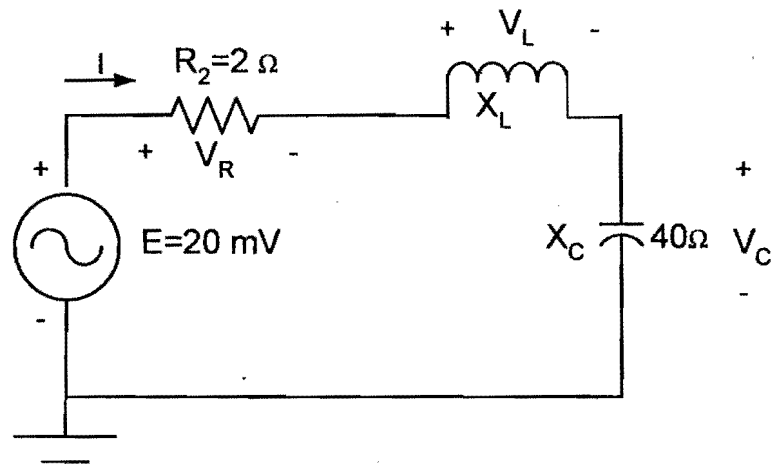


Fig.Q5b

### QUESTION 6

(a) Given that  $v(t) = 120\cos(314t + 45^\circ)\text{V}$  and  $i(t) = 10\cos(314t - 10^\circ)\text{A}$  at the terminals of a passive linear network,

- Draw the voltage and current waveforms. [2 marks]
- Mention the types of the network and give reason of your answer. [2 mark]
- Find the instantaneous power, the average power, reactive power and apparent powers absorbed by the network. [4 marks]

(b) For the network shown in Fig. Q6b

- Find  $Z_T$  and  $Y_T$ . [4 marks]
- Find currents  $I_1$  and  $I_2$ ,  $I_3$  and  $I$ . [2x4=8 marks]
- Verify Kirchhoff's current law by showing that  $I = I_1 + I_2 + I_3$ . [2 marks]
- Use complex conjugate method to calculate power and hence draw the power triangle. [3 marks]

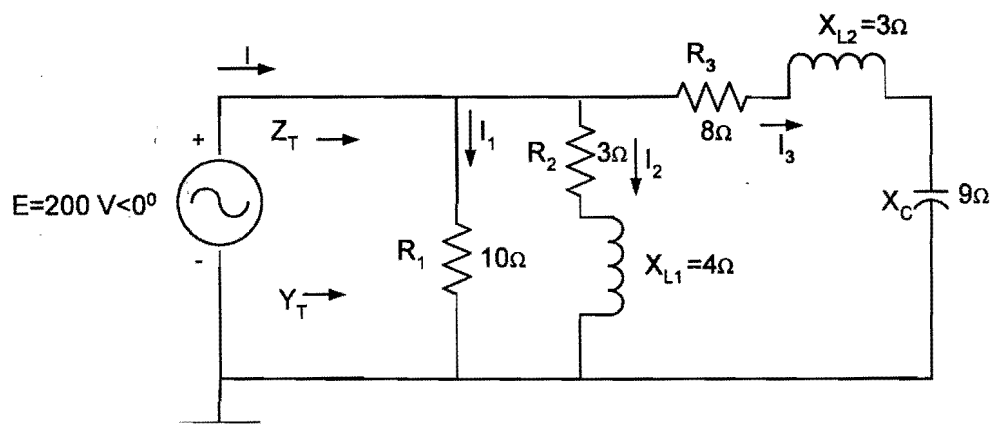


Fig. Q6b

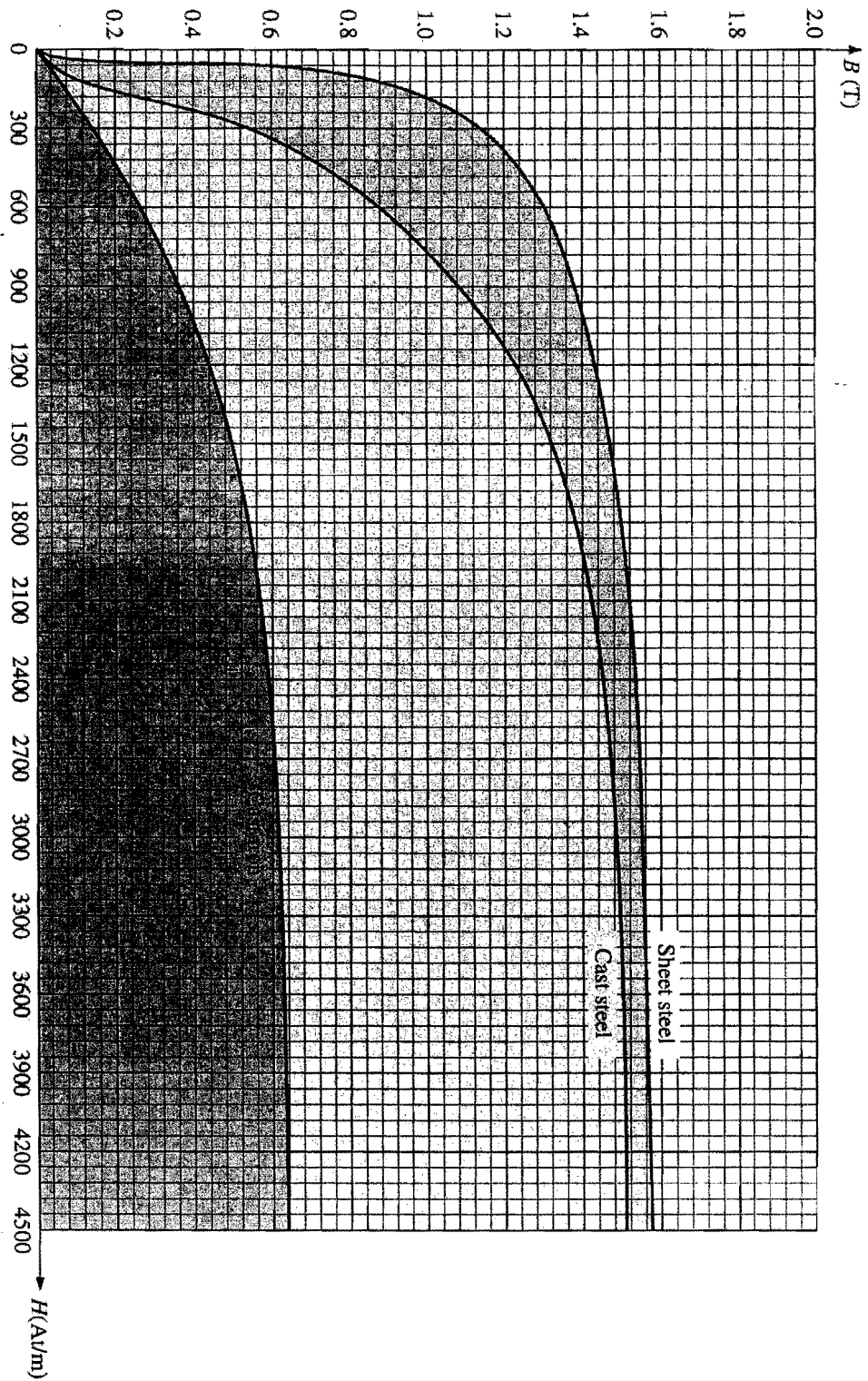


Fig. B-H curve needed for Q 4(a)  
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