

UNIVERSITY OF SWAZILAND
FACULTY OF SCIENCE & ENGINEERING
DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING

MAIN EXAMINATION DECEMBER 2012

TITLE OF PAPER: ELECTROMAGNETIC FIELDS II

COURSE CODE: EE441

TIME ALLOWED: THREE HOURS

INSTRUCTIONS:

1. Answer any **four (4) questions**
2. Each question carries 25 marks.
3. Marks for different sections are shown in the right-hand margin.

This paper has 3 pages including this page.

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Question 1

Use a Smith chart to determine the input impedance Z_{in} of the feed line for the lossless transmission line shown below in Figure 1. All lines have the characteristic impedance of $Z_0 = 50 \Omega$. (25 marks)

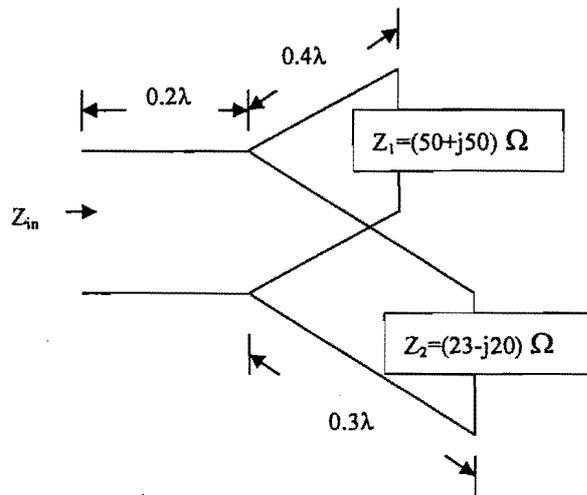


Figure 1

Question 2

A 90 millimeter section of a 50Ω transmission line is driven by a source with $v_g(t) = 12 \cos(6\pi \times 10^9 t - 36.937^\circ)$ (V) and $Z_g = 50 \Omega$, is terminated in a load $Z_L = (75 - j100) \Omega$.

Determine:

- λ on the line, (2 marks)
- the reflection coefficient at the load, (4 marks)
- the voltage standing wave ratio, (2 marks)
- the input impedance, and (8 marks)
- the input voltage $v_i(t)$. (9 marks)

Question 3

A beam of light with wavelength $0.6 \mu\text{m}$ is normally incident in air upon a glass surface. If the surface is situated in the plane $z = 0$ and the relative permittivity of glass is 2.25, determine:

- the intrinsic impedances η_1 and η_2 , (6 marks)
- the reflection coefficient Γ , (3 marks)
- the location of the electric field maxima in medium 1 (air), and (4 marks)
- the fraction of the incident power transmitted into the glass medium. (12 marks)

Question 4

In a medium with $\epsilon = 36\epsilon_0$ and $\mu = \mu_0$ the electric field intensity of an electromagnetic wave is

$$\tilde{\mathbf{E}} = (\hat{x} + j\hat{y})30e^{-jkz} \text{ (V/m)}.$$

Determine the associated time-harmonic magnetic field intensity $\mathbf{H}(z,t)$ and find the value of k . (25 marks)

Question 5

A TM wave propagating in a dielectric-filled waveguide of unknown permittivity has a magnetic field with y-component given by

$$H_y = 10 \cos(50\pi x) \sin(100\pi y) \times \sin(1.5\pi \times 10^{10} t - 100\pi z) \text{ (mA/m)}.$$

If the guide dimensions are $a = 2b = 2$ cm, determine:

- a) the mode numbers, (4 marks)
- b) the relative permittivity of the material in the guide, (7 marks)
- c) the phase velocity, (2 marks)
- d) obtain an expression for E_x . (12 marks)

