

UNIVERSITY OF SWAZILAND  
FACULTY OF SOCIAL SCIENCES  
DEPARTMENT OF ECONOMICS  
RE-SIT EXAMINATION JULY 2018

**TITLE OF PAPER : INTRODUCTION TO ECONOMETRICS I**  
**COURSE CODE : ECO 307**  
**TIME ALLOWED : TWO (2) HOURS**

**INSTRUCTIONS :**

- 1. ANSWER QUESTION ONE (1) AND ANY OTHER TWO (2) IN THIS PAPER.**
- 2. ONLY SCIENTIFIC NON-PROGRAMMABLE CALCULATORS ARE ALLOWED.**
- 3. ROUND UP YOUR FINAL ANSWERS TO THREE (3) DECIMAL PLACES.**
- 4. IF IT IS NOT SPECIFIED, USE  $\alpha = 0.05$  FOR STATISTICAL TESTS.**
- 5. THE REQUIRED PROBABILITY TABLES ARE ATTACHED AT THE BACK OF QUESTION PAPER.**

**THIS PAPER IS NOT TO BE OPENED UNTIL PERMISSION HAS BEEN GRANTED BY THE INVIGILATOR**

**QUESTION 1 (Compulsory)****[40 MARKS]**

- a) Differentiate between time series and panel data. [6 Marks]  
 b) State the Gauss-Markov theorem. [6 Marks]  
 c) The table below shows sample data of CEO salaries ( $y$ ) in Emalangeni and the companies' return on equity (ROE) ( $x$ ) in percentages:

|        |      |      |      |     |      |      |      |      |      |      |
|--------|------|------|------|-----|------|------|------|------|------|------|
| Salary | 1095 | 1001 | 1122 | 578 | 1368 | 1145 | 1078 | 1094 | 1237 | 833  |
| ROE    | 14.1 | 10.9 | 23.5 | 5.9 | 13.8 | 20   | 16.4 | 16.3 | 10.5 | 26.3 |

- i) Use the data to fit a regression line. (Show working for full marks) [16 Marks]  
 ii) Interpret the slope coefficient of the regression. [6 Marks]  
 iii) If the calculated coefficient of determination ( $R^2$ ) for the above data is 0.2052, interpret what it means. [6 Marks]

**ANSWER ANY TWO QUESTIONS FROM THE FOLLOWING QUESTIONS****QUESTION 2****[25 MARKS]**

Consider an estimated model for the number of defective products ( $Defect$ ) per 100 units of production, for a citrus canning factory in Malkerns.  $Hrsemp$  is the total training hours provided to employees, and  $Employ$  is the number of workers in a shift.

$$\begin{aligned} \widehat{\text{Log}(Defect)} &= 11.74 + 0.42Hrsemp - 0.083 \log(Employ) \\ &\quad (4.57) \quad (0.019) \quad (0.360) \\ n &= 43, \quad R^2 = 0.310 \end{aligned}$$

Note that the values in brackets are standard errors.

- a) Interpret the model. [6 Marks]  
 b) Briefly explain whether the signs of the coefficients make sense. [5 Marks]  
 c) Using the standard normal table approximation, find the 95% confidence interval for  $\beta_{Hrsemp}$ . [8 Marks]  
 d) Are you able to reject the null hypothesis  $H_0 : \beta_{Hrsemp} = 0$  at the 5% level of significance? [5 Marks]

- e) What is the  $p$  – value that can be attached on coefficient of the log of the number of workers working in a shift ( $\beta_{Log(Employ)}$ ). [6 Marks]

### **QUESTION 3**

**[30 MARKS]**

The following output was obtained from running a model of the following form in Stata :

$$y_i = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + u_i$$

| Source   | SS       | df   | MS         | Number of Obs = | 1388   |
|----------|----------|------|------------|-----------------|--------|
| Model    | 17126.21 | 2    | 8563.10442 | F(3, 522) =     | 21.27  |
| Residual | 557485.5 | 1385 | 402.516614 | Prob > F =      | 0.0000 |
| Total    | 574611.7 | 1387 | 414.283864 | R - Squared =   |        |

Root MSE = 20.063

| bwght    | Coef.    | Std. Err. | t      | P>t   | [95% Conf. Interval] |
|----------|----------|-----------|--------|-------|----------------------|
| cigs     | -0.46341 | 0.091577  | -5.06  | 0.000 | -0.64305 -0.283763   |
| faminc   | 0.092765 | 0.029188  | 3.18   | 0.002 | 0.035508 0.1500219   |
| Constant | 116.9741 | 1.048984  | 111.51 | 0.000 | 114.9164 119.0319    |

Where **bwght** – birth weight of child, **cigs** – number of cigarettes smoked per day while pregnant, **faminc** – family income in Thousand Emalangeni.

- a) State the fitted regression line. [3 Marks]
- b) Interpret the coefficient  $\beta_{cigs}$  [6 Marks]
- c) Perform the  $F$  – Test for the above model and clearly state your conclusion. [5 Marks]
- d) Test the hypothesis that  $\beta_{Constant} = 0$  against  $\beta_{Constant} \neq 0$  at the 1% level of significance. [5 Marks]
- e) Does the data provide evidence that *faminc* contributes useful information in the prediction of the birth weight of a child? [6 Marks]
- f) Calculate the Goodness of Fit measure ( $R^2$ ) and interpret it. [5 Marks]

**QUESTION 4****[30 MARKS]**

- a) Briefly explain why in some models it is necessary to include an interaction of the independent variables. [6 Marks]
- b) Consider the following model whereby the returns to education depend upon the amount of work experience.

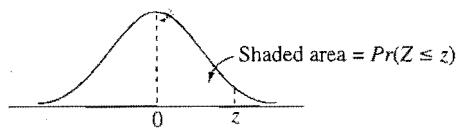
$$\log(wage) = \beta_0 + \beta_1 educ + \beta_2 exper + \beta_3 educ * exper + u$$

Where wage – monthly wage, educ – education in years, exper – years of work experience

- a) If experience is held constant, what is the effect of education? [6 Marks]
- b) State the null hypothesis that the return to education does not depend on the level of experience. State and **justify** an appropriate alternative hypothesis. [6 Marks]
- c) If the model in (b) above is estimated as :

$$\begin{aligned} \widehat{\log(wage)} &= 5.9494 + 0.044 \text{ educ} - 0.0215 \text{ exper} + 0.0032 \text{ educ * exper} \\ &\quad (0.2408) \quad (0.0174) \quad (0.020) \quad (0.0015) \\ n &= 935, \quad R^2 = 0.1349 \end{aligned}$$

- d) Test the hypotheses you stated in (b) above. [7 Marks]
- e) Is it necessary to include the interaction term ( $educ * exper$ ) in the model? [5 Marks]



**TABLE 1**  
Standard normal curve areas

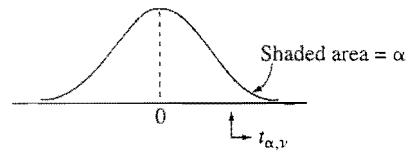
| <i>z</i> | 0.00       | 0.01   | 0.02   | 0.03   | 0.04   | 0.05   | 0.06   | 0.07   | 0.08   | 0.09   |
|----------|------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| -3.4     | 0.0003     | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0002 |
| -3.3     | 0.0005     | 0.0005 | 0.0005 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0003 |
| -3.2     | 0.0007     | 0.0007 | 0.0006 | 0.0006 | 0.0006 | 0.0006 | 0.0006 | 0.0005 | 0.0005 | 0.0005 |
| -3.1     | 0.0010     | 0.0009 | 0.0009 | 0.0009 | 0.0008 | 0.0008 | 0.0008 | 0.0008 | 0.0007 | 0.0007 |
| -3.0     | 0.0013     | 0.0013 | 0.0013 | 0.0012 | 0.0012 | 0.0011 | 0.0011 | 0.0011 | 0.0010 | 0.0010 |
| -2.9     | 0.0019     | 0.0018 | 0.0018 | 0.0017 | 0.0016 | 0.0016 | 0.0015 | 0.0015 | 0.0014 | 0.0014 |
| -2.8     | 0.0026     | 0.0025 | 0.0024 | 0.0023 | 0.0023 | 0.0022 | 0.0021 | 0.0021 | 0.0020 | 0.0019 |
| -2.7     | 0.0035     | 0.0034 | 0.0033 | 0.0032 | 0.0031 | 0.0030 | 0.0029 | 0.0028 | 0.0027 | 0.0026 |
| -2.6     | 0.0047     | 0.0045 | 0.0044 | 0.0043 | 0.0041 | 0.0040 | 0.0039 | 0.0038 | 0.0037 | 0.0036 |
| -2.5     | 0.0062     | 0.0060 | 0.0059 | 0.0057 | 0.0055 | 0.0054 | 0.0052 | 0.0051 | 0.0049 | 0.0048 |
| -2.4     | 0.0082     | 0.0080 | 0.0078 | 0.0075 | 0.0073 | 0.0071 | 0.0069 | 0.0068 | 0.0066 | 0.0064 |
| -2.3     | 0.0107     | 0.0104 | 0.0102 | 0.0099 | 0.0096 | 0.0094 | 0.0091 | 0.0089 | 0.0087 | 0.0084 |
| -2.2     | 0.0139     | 0.0136 | 0.0132 | 0.0129 | 0.0125 | 0.0122 | 0.0119 | 0.0116 | 0.0113 | 0.0110 |
| -2.1     | 0.0179     | 0.0174 | 0.0170 | 0.0166 | 0.0162 | 0.0158 | 0.0154 | 0.0150 | 0.0146 | 0.0143 |
| -2.0     | 0.0228     | 0.0222 | 0.0217 | 0.0212 | 0.0207 | 0.0202 | 0.0197 | 0.0192 | 0.0188 | 0.0183 |
| -1.9     | 0.0287     | 0.0281 | 0.0274 | 0.0268 | 0.0262 | 0.0256 | 0.0250 | 0.0244 | 0.0239 | 0.0233 |
| -1.8     | 0.0359     | 0.0351 | 0.0344 | 0.0336 | 0.0329 | 0.0322 | 0.0314 | 0.0307 | 0.0301 | 0.0294 |
| -1.7     | 0.0446     | 0.0436 | 0.0427 | 0.0418 | 0.0409 | 0.0401 | 0.0392 | 0.0384 | 0.0375 | 0.0367 |
| -1.6     | 0.0548     | 0.0537 | 0.0526 | 0.0516 | 0.0505 | 0.0495 | 0.0485 | 0.0475 | 0.0465 | 0.0455 |
| -1.5     | 0.0668     | 0.0655 | 0.0643 | 0.0630 | 0.0618 | 0.0606 | 0.0594 | 0.0582 | 0.0571 | 0.0559 |
| -1.4     | 0.0808     | 0.0793 | 0.0778 | 0.0764 | 0.0749 | 0.0735 | 0.0721 | 0.0708 | 0.0694 | 0.0681 |
| -1.3     | 0.0968     | 0.0951 | 0.0934 | 0.0918 | 0.0901 | 0.0885 | 0.0869 | 0.0853 | 0.0838 | 0.0823 |
| -1.2     | 0.1151     | 0.1131 | 0.1112 | 0.1093 | 0.1075 | 0.1056 | 0.1038 | 0.1020 | 0.1003 | 0.0985 |
| -1.1     | 0.1357     | 0.1335 | 0.1314 | 0.1292 | 0.1271 | 0.1251 | 0.1230 | 0.1210 | 0.1190 | 0.1170 |
| -1.0     | 0.1587     | 0.1562 | 0.1539 | 0.1515 | 0.1492 | 0.1469 | 0.1446 | 0.1423 | 0.1401 | 0.1379 |
| -0.9     | 0.1841     | 0.1814 | 0.1788 | 0.1762 | 0.1736 | 0.1711 | 0.1685 | 0.1660 | 0.1635 | 0.1611 |
| -0.8     | 0.2119     | 0.2090 | 0.2061 | 0.2033 | 0.2005 | 0.1977 | 0.1949 | 0.1922 | 0.1894 | 0.1867 |
| -0.7     | 0.2420     | 0.2389 | 0.2358 | 0.2327 | 0.2296 | 0.2266 | 0.2236 | 0.2206 | 0.2177 | 0.2148 |
| -0.6     | 0.2743     | 0.2709 | 0.2676 | 0.2643 | 0.2611 | 0.2578 | 0.2546 | 0.2514 | 0.2483 | 0.2451 |
| -0.5     | 0.3085     | 0.3050 | 0.3015 | 0.2981 | 0.2946 | 0.2912 | 0.2877 | 0.2843 | 0.2810 | 0.2776 |
| -0.4     | 0.3446     | 0.3409 | 0.3372 | 0.3336 | 0.3300 | 0.3264 | 0.3228 | 0.3192 | 0.3156 | 0.3121 |
| -0.3     | 0.3821     | 0.3783 | 0.3745 | 0.3707 | 0.3669 | 0.3632 | 0.3594 | 0.3557 | 0.3520 | 0.3483 |
| -0.2     | 0.4207     | 0.4168 | 0.4129 | 0.4090 | 0.4052 | 0.4013 | 0.3974 | 0.3936 | 0.3897 | 0.3859 |
| -0.1     | 0.4602     | 0.4562 | 0.4522 | 0.4483 | 0.4443 | 0.4404 | 0.4364 | 0.4325 | 0.4286 | 0.4247 |
| -0.0     | 0.5000     | 0.4960 | 0.4920 | 0.4880 | 0.4840 | 0.4801 | 0.4761 | 0.4721 | 0.4681 | 0.4641 |
| <i>z</i> | Area       |        |        |        |        |        |        |        |        |        |
| -3.50    | 0.00023263 |        |        |        |        |        |        |        |        |        |
| -4.00    | 0.00003167 |        |        |        |        |        |        |        |        |        |
| -4.50    | 0.00000340 |        |        |        |        |        |        |        |        |        |
| -5.00    | 0.00000029 |        |        |        |        |        |        |        |        |        |

Source: Computed by M. Longnecker using Splus.

**1092 Appendix**
**TABLE 1**  
 Standard normal curve areas

| <i>z</i> | 0.00   | 0.01   | 0.02   | 0.03   | 0.04   | 0.05   | 0.06   | 0.07   | 0.08   | 0.09   |
|----------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0.0      | 0.5000 | 0.5040 | 0.5080 | 0.5120 | 0.5160 | 0.5199 | 0.5239 | 0.5279 | 0.5319 | 0.5359 |
| 0.1      | 0.5398 | 0.5438 | 0.5478 | 0.5517 | 0.5557 | 0.5596 | 0.5636 | 0.5675 | 0.5714 | 0.5753 |
| 0.2      | 0.5793 | 0.5832 | 0.5871 | 0.5910 | 0.5948 | 0.5987 | 0.6026 | 0.6064 | 0.6103 | 0.6141 |
| 0.3      | 0.6179 | 0.6217 | 0.6255 | 0.6293 | 0.6331 | 0.6368 | 0.6406 | 0.6443 | 0.6480 | 0.6517 |
| 0.4      | 0.6554 | 0.6591 | 0.6628 | 0.6664 | 0.6700 | 0.6736 | 0.6772 | 0.6808 | 0.6844 | 0.6879 |
| 0.5      | 0.6915 | 0.6950 | 0.6985 | 0.7019 | 0.7054 | 0.7088 | 0.7123 | 0.7157 | 0.7190 | 0.7224 |
| 0.6      | 0.7257 | 0.7291 | 0.7324 | 0.7357 | 0.7389 | 0.7422 | 0.7454 | 0.7486 | 0.7517 | 0.7549 |
| 0.7      | 0.7580 | 0.7611 | 0.7642 | 0.7673 | 0.7704 | 0.7734 | 0.7764 | 0.7794 | 0.7823 | 0.7852 |
| 0.8      | 0.7881 | 0.7910 | 0.7939 | 0.7967 | 0.7995 | 0.8023 | 0.8051 | 0.8078 | 0.8106 | 0.8133 |
| 0.9      | 0.8159 | 0.8186 | 0.8212 | 0.8238 | 0.8264 | 0.8289 | 0.8315 | 0.8340 | 0.8365 | 0.8389 |
| 1.0      | 0.8413 | 0.8438 | 0.8461 | 0.8485 | 0.8508 | 0.8531 | 0.8554 | 0.8577 | 0.8599 | 0.8621 |
| 1.1      | 0.8643 | 0.8665 | 0.8686 | 0.8708 | 0.8729 | 0.8749 | 0.8770 | 0.8790 | 0.8810 | 0.8830 |
| 1.2      | 0.8849 | 0.8869 | 0.8888 | 0.8907 | 0.8925 | 0.8944 | 0.8962 | 0.8980 | 0.8997 | 0.9015 |
| 1.3      | 0.9032 | 0.9049 | 0.9066 | 0.9082 | 0.9099 | 0.9115 | 0.9131 | 0.9147 | 0.9162 | 0.9177 |
| 1.4      | 0.9192 | 0.9207 | 0.9222 | 0.9236 | 0.9251 | 0.9265 | 0.9279 | 0.9292 | 0.9306 | 0.9319 |
| 1.5      | 0.9332 | 0.9345 | 0.9357 | 0.9370 | 0.9382 | 0.9394 | 0.9406 | 0.9418 | 0.9429 | 0.9441 |
| 1.6      | 0.9452 | 0.9463 | 0.9474 | 0.9484 | 0.9495 | 0.9505 | 0.9515 | 0.9525 | 0.9535 | 0.9545 |
| 1.7      | 0.9554 | 0.9564 | 0.9573 | 0.9582 | 0.9591 | 0.9599 | 0.9608 | 0.9616 | 0.9625 | 0.9633 |
| 1.8      | 0.9641 | 0.9649 | 0.9656 | 0.9664 | 0.9671 | 0.9678 | 0.9686 | 0.9693 | 0.9699 | 0.9706 |
| 1.9      | 0.9713 | 0.9719 | 0.9726 | 0.9732 | 0.9738 | 0.9744 | 0.9750 | 0.9756 | 0.9761 | 0.9767 |
| 2.0      | 0.9772 | 0.9778 | 0.9783 | 0.9788 | 0.9793 | 0.9798 | 0.9803 | 0.9808 | 0.9812 | 0.9817 |
| 2.1      | 0.9821 | 0.9826 | 0.9830 | 0.9834 | 0.9838 | 0.9842 | 0.9846 | 0.9850 | 0.9854 | 0.9857 |
| 2.2      | 0.9861 | 0.9864 | 0.9868 | 0.9871 | 0.9875 | 0.9878 | 0.9881 | 0.9884 | 0.9887 | 0.9890 |
| 2.3      | 0.9893 | 0.9896 | 0.9898 | 0.9901 | 0.9904 | 0.9906 | 0.9909 | 0.9911 | 0.9913 | 0.9916 |
| 2.4      | 0.9918 | 0.9920 | 0.9922 | 0.9925 | 0.9927 | 0.9929 | 0.9931 | 0.9932 | 0.9934 | 0.9936 |
| 2.5      | 0.9938 | 0.9940 | 0.9941 | 0.9943 | 0.9945 | 0.9946 | 0.9948 | 0.9949 | 0.9951 | 0.9952 |
| 2.6      | 0.9953 | 0.9955 | 0.9956 | 0.9957 | 0.9959 | 0.9960 | 0.9961 | 0.9962 | 0.9963 | 0.9964 |
| 2.7      | 0.9965 | 0.9966 | 0.9967 | 0.9968 | 0.9969 | 0.9970 | 0.9971 | 0.9972 | 0.9973 | 0.9974 |
| 2.8      | 0.9974 | 0.9975 | 0.9976 | 0.9977 | 0.9977 | 0.9978 | 0.9979 | 0.9979 | 0.9980 | 0.9981 |
| 2.9      | 0.9981 | 0.9982 | 0.9982 | 0.9983 | 0.9984 | 0.9984 | 0.9985 | 0.9985 | 0.9986 | 0.9986 |
| 3.0      | 0.9987 | 0.9987 | 0.9987 | 0.9988 | 0.9988 | 0.9989 | 0.9989 | 0.9989 | 0.9990 | 0.9990 |
| 3.1      | 0.9990 | 0.9991 | 0.9991 | 0.9991 | 0.9992 | 0.9992 | 0.9992 | 0.9992 | 0.9993 | 0.9993 |
| 3.2      | 0.9993 | 0.9993 | 0.9994 | 0.9994 | 0.9994 | 0.9994 | 0.9994 | 0.9995 | 0.9995 | 0.9995 |
| 3.3      | 0.9995 | 0.9995 | 0.9995 | 0.9996 | 0.9996 | 0.9996 | 0.9996 | 0.9996 | 0.9996 | 0.9997 |
| 3.4      | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9998 |

| <i>z</i> | Area       |
|----------|------------|
| 3.50     | 0.99976737 |
| 4.00     | 0.99996833 |
| 4.50     | 0.99999660 |
| 5.00     | 0.99999971 |



**TABLE 2**  
Percentage points of Student's  $t$  distribution

| df/ $\alpha$ | .40   | .25   | .10   | .05   | .025   | .01    | .005   | .001    | .0005   |
|--------------|-------|-------|-------|-------|--------|--------|--------|---------|---------|
| 1            | 0.325 | 1.000 | 3.078 | 6.314 | 12.706 | 31.821 | 63.657 | 318.309 | 636.619 |
| 2            | 0.289 | 0.816 | 1.886 | 2.920 | 4.303  | 6.965  | 9.925  | 22.327  | 31.599  |
| 3            | 0.277 | 0.765 | 1.638 | 2.353 | 3.182  | 4.541  | 5.841  | 10.215  | 12.924  |
| 4            | 0.271 | 0.741 | 1.533 | 2.132 | 2.776  | 3.747  | 4.604  | 7.173   | 8.610   |
| 5            | 0.267 | 0.727 | 1.476 | 2.015 | 2.571  | 3.365  | 4.032  | 5.893   | 6.869   |
| 6            | 0.265 | 0.718 | 1.440 | 1.943 | 2.447  | 3.143  | 3.707  | 5.208   | 5.959   |
| 7            | 0.263 | 0.711 | 1.415 | 1.895 | 2.365  | 2.998  | 3.499  | 4.785   | 5.408   |
| 8            | 0.262 | 0.706 | 1.397 | 1.860 | 2.306  | 2.896  | 3.355  | 4.501   | 5.041   |
| 9            | 0.261 | 0.703 | 1.383 | 1.833 | 2.262  | 2.821  | 3.250  | 4.297   | 4.781   |
| 10           | 0.260 | 0.700 | 1.372 | 1.812 | 2.228  | 2.764  | 3.169  | 4.144   | 4.587   |
| 11           | 0.260 | 0.697 | 1.363 | 1.796 | 2.201  | 2.718  | 3.106  | 4.025   | 4.437   |
| 12           | 0.259 | 0.695 | 1.356 | 1.782 | 2.179  | 2.681  | 3.055  | 3.930   | 4.318   |
| 13           | 0.259 | 0.694 | 1.350 | 1.771 | 2.160  | 2.650  | 3.012  | 3.852   | 4.221   |
| 14           | 0.258 | 0.692 | 1.345 | 1.761 | 2.145  | 2.624  | 2.977  | 3.787   | 4.140   |
| 15           | 0.258 | 0.691 | 1.341 | 1.753 | 2.131  | 2.602  | 2.947  | 3.733   | 4.073   |
| 16           | 0.258 | 0.690 | 1.337 | 1.746 | 2.120  | 2.583  | 2.921  | 3.686   | 4.015   |
| 17           | 0.257 | 0.689 | 1.333 | 1.740 | 2.110  | 2.567  | 2.898  | 3.646   | 3.965   |
| 18           | 0.257 | 0.688 | 1.330 | 1.734 | 2.101  | 2.552  | 2.878  | 3.610   | 3.922   |
| 19           | 0.257 | 0.688 | 1.328 | 1.729 | 2.093  | 2.539  | 2.861  | 3.579   | 3.883   |
| 20           | 0.257 | 0.687 | 1.325 | 1.725 | 2.086  | 2.528  | 2.845  | 3.552   | 3.850   |
| 21           | 0.257 | 0.686 | 1.323 | 1.721 | 2.080  | 2.518  | 2.831  | 3.527   | 3.819   |
| 22           | 0.256 | 0.686 | 1.321 | 1.717 | 2.074  | 2.508  | 2.819  | 3.505   | 3.792   |
| 23           | 0.256 | 0.685 | 1.319 | 1.714 | 2.069  | 2.500  | 2.807  | 3.485   | 3.768   |
| 24           | 0.256 | 0.685 | 1.318 | 1.711 | 2.064  | 2.492  | 2.797  | 3.467   | 3.745   |
| 25           | 0.256 | 0.684 | 1.316 | 1.708 | 2.060  | 2.485  | 2.787  | 3.450   | 3.725   |
| 26           | 0.256 | 0.684 | 1.315 | 1.706 | 2.056  | 2.479  | 2.779  | 3.435   | 3.707   |
| 27           | 0.256 | 0.684 | 1.314 | 1.703 | 2.052  | 2.473  | 2.771  | 3.421   | 3.690   |
| 28           | 0.256 | 0.683 | 1.313 | 1.701 | 2.048  | 2.467  | 2.763  | 3.408   | 3.674   |
| 29           | 0.256 | 0.683 | 1.311 | 1.699 | 2.045  | 2.462  | 2.756  | 3.396   | 3.659   |
| 30           | 0.256 | 0.683 | 1.310 | 1.697 | 2.042  | 2.457  | 2.750  | 3.385   | 3.646   |
| 35           | 0.255 | 0.682 | 1.306 | 1.690 | 2.030  | 2.438  | 2.724  | 3.340   | 3.591   |
| 40           | 0.255 | 0.681 | 1.303 | 1.684 | 2.021  | 2.423  | 2.704  | 3.307   | 3.551   |
| 50           | 0.255 | 0.679 | 1.299 | 1.676 | 2.009  | 2.403  | 2.678  | 3.261   | 3.496   |
| 60           | 0.254 | 0.679 | 1.296 | 1.671 | 2.000  | 2.390  | 2.660  | 3.232   | 3.460   |
| 120          | 0.254 | 0.677 | 1.289 | 1.658 | 1.980  | 2.358  | 2.617  | 3.160   | 3.373   |
| inf.         | 0.253 | 0.674 | 1.282 | 1.645 | 1.960  | 2.326  | 2.576  | 3.090   | 3.291   |

Source: Computed by M. Longnecker using Splus.

TABLE A.3

*F* Distribution: Critical Values of *F* (5% significance level)

| $v_1$ | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | 10     | 12     | 14     | 16     | 18     | 20     |
|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| $v_2$ |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |
| 1     | 161.45 | 199.50 | 215.71 | 224.58 | 230.16 | 233.99 | 236.77 | 238.88 | 240.54 | 241.88 | 243.91 | 245.36 | 246.46 | 247.32 | 248.01 |
| 2     | 18.51  | 19.00  | 19.16  | 19.25  | 19.30  | 19.33  | 19.35  | 19.37  | 19.38  | 19.40  | 19.41  | 19.42  | 19.43  | 19.44  | 19.45  |
| 3     | 10.13  | 9.55   | 9.28   | 9.12   | 9.01   | 8.94   | 8.89   | 8.85   | 8.81   | 8.79   | 8.74   | 8.71   | 8.69   | 8.67   | 8.66   |
| 4     | 7.71   | 6.94   | 6.59   | 6.39   | 6.26   | 6.16   | 6.09   | 6.04   | 6.00   | 5.96   | 5.91   | 5.87   | 5.84   | 5.82   | 5.80   |
| 5     | 6.61   | 5.79   | 5.41   | 5.19   | 5.05   | 4.95   | 4.88   | 4.82   | 4.77   | 4.74   | 4.68   | 4.64   | 4.60   | 4.58   | 4.56   |
| 6     | 5.99   | 5.14   | 4.76   | 4.53   | 4.39   | 4.28   | 4.21   | 4.15   | 4.10   | 4.06   | 4.00   | 3.96   | 3.92   | 3.90   | 3.87   |
| 7     | 5.59   | 4.74   | 4.35   | 4.12   | 3.97   | 3.87   | 3.79   | 3.73   | 3.68   | 3.64   | 3.57   | 3.53   | 3.49   | 3.47   | 3.44   |
| 8     | 5.32   | 4.46   | 4.07   | 3.84   | 3.69   | 3.58   | 3.50   | 3.44   | 3.39   | 3.35   | 3.28   | 3.24   | 3.20   | 3.17   | 3.15   |
| 9     | 5.12   | 4.26   | 3.86   | 3.63   | 3.48   | 3.37   | 3.29   | 3.23   | 3.18   | 3.14   | 3.07   | 3.03   | 2.99   | 2.96   | 2.94   |
| 10    | 4.96   | 4.10   | 3.71   | 3.48   | 3.33   | 3.22   | 3.14   | 3.07   | 3.02   | 2.98   | 2.91   | 2.86   | 2.83   | 2.80   | 2.77   |
| 11    | 4.84   | 3.98   | 3.59   | 3.36   | 3.20   | 3.09   | 3.01   | 2.95   | 2.90   | 2.85   | 2.79   | 2.74   | 2.70   | 2.67   | 2.65   |
| 12    | 4.75   | 3.89   | 3.49   | 3.26   | 3.11   | 3.00   | 2.91   | 2.85   | 2.80   | 2.75   | 2.69   | 2.64   | 2.60   | 2.57   | 2.54   |
| 13    | 4.67   | 3.81   | 3.41   | 3.18   | 3.03   | 2.92   | 2.83   | 2.77   | 2.71   | 2.67   | 2.60   | 2.55   | 2.51   | 2.48   | 2.46   |
| 14    | 4.60   | 3.74   | 3.34   | 3.11   | 2.96   | 2.85   | 2.76   | 2.70   | 2.65   | 2.60   | 2.53   | 2.48   | 2.44   | 2.41   | 2.39   |
| 15    | 4.54   | 3.68   | 3.29   | 3.06   | 2.90   | 2.79   | 2.71   | 2.64   | 2.59   | 2.54   | 2.48   | 2.42   | 2.38   | 2.35   | 2.33   |
| 16    | 4.49   | 3.63   | 3.24   | 3.01   | 2.85   | 2.74   | 2.66   | 2.59   | 2.54   | 2.49   | 2.42   | 2.37   | 2.33   | 2.30   | 2.28   |
| 17    | 4.45   | 3.59   | 3.20   | 2.96   | 2.81   | 2.70   | 2.61   | 2.55   | 2.49   | 2.45   | 2.38   | 2.33   | 2.29   | 2.26   | 2.23   |
| 18    | 4.41   | 3.55   | 3.16   | 2.93   | 2.77   | 2.66   | 2.58   | 2.51   | 2.46   | 2.41   | 2.34   | 2.29   | 2.25   | 2.22   | 2.19   |
| 19    | 4.38   | 3.52   | 3.13   | 2.90   | 2.74   | 2.63   | 2.54   | 2.48   | 2.42   | 2.38   | 2.31   | 2.26   | 2.21   | 2.18   | 2.16   |
| 20    | 4.35   | 3.49   | 3.10   | 2.87   | 2.71   | 2.60   | 2.51   | 2.45   | 2.39   | 2.35   | 2.28   | 2.22   | 2.18   | 2.15   | 2.12   |
| 21    | 4.32   | 3.47   | 3.07   | 2.84   | 2.68   | 2.57   | 2.49   | 2.42   | 2.37   | 2.32   | 2.25   | 2.20   | 2.16   | 2.12   | 2.10   |
| 22    | 4.30   | 3.44   | 3.05   | 2.82   | 2.66   | 2.55   | 2.46   | 2.40   | 2.34   | 2.30   | 2.23   | 2.17   | 2.13   | 2.10   | 2.07   |
| 23    | 4.28   | 3.42   | 3.03   | 2.80   | 2.64   | 2.53   | 2.44   | 2.37   | 2.32   | 2.27   | 2.20   | 2.15   | 2.11   | 2.08   | 2.05   |
| 24    | 4.26   | 3.40   | 3.01   | 2.78   | 2.62   | 2.51   | 2.42   | 2.36   | 2.30   | 2.25   | 2.18   | 2.13   | 2.09   | 2.05   | 2.03   |
| 25    | 4.24   | 3.39   | 2.99   | 2.76   | 2.60   | 2.49   | 2.40   | 2.34   | 2.28   | 2.24   | 2.16   | 2.11   | 2.07   | 2.04   | 2.01   |
| 26    | 4.22   | 3.37   | 2.98   | 2.74   | 2.59   | 2.47   | 2.39   | 2.32   | 2.27   | 2.22   | 2.15   | 2.09   | 2.05   | 2.02   | 1.99   |
| 27    | 4.21   | 3.35   | 2.96   | 2.73   | 2.57   | 2.46   | 2.37   | 2.31   | 2.25   | 2.20   | 2.13   | 2.08   | 2.04   | 2.00   | 1.97   |
| 28    | 4.20   | 3.34   | 2.95   | 2.71   | 2.56   | 2.45   | 2.36   | 2.29   | 2.24   | 2.19   | 2.12   | 2.06   | 2.02   | 1.99   | 1.96   |
| 29    | 4.18   | 3.33   | 2.93   | 2.70   | 2.55   | 2.43   | 2.35   | 2.28   | 2.22   | 2.18   | 2.10   | 2.05   | 2.01   | 1.97   | 1.94   |
| 30    | 4.17   | 3.32   | 2.92   | 2.69   | 2.53   | 2.42   | 2.33   | 2.27   | 2.21   | 2.16   | 2.09   | 2.04   | 1.99   | 1.96   | 1.93   |
| 35    | 4.12   | 3.27   | 2.87   | 2.64   | 2.49   | 2.37   | 2.29   | 2.22   | 2.16   | 2.11   | 2.04   | 1.99   | 1.94   | 1.91   | 1.88   |
| 40    | 4.08   | 3.23   | 2.84   | 2.61   | 2.45   | 2.34   | 2.25   | 2.18   | 2.12   | 2.08   | 2.00   | 1.95   | 1.90   | 1.87   | 1.84   |
| 50    | 4.03   | 3.18   | 2.79   | 2.56   | 2.40   | 2.29   | 2.20   | 2.13   | 2.07   | 2.03   | 1.95   | 1.89   | 1.85   | 1.81   | 1.78   |
| 60    | 4.00   | 3.15   | 2.76   | 2.53   | 2.37   | 2.25   | 2.17   | 2.10   | 2.04   | 1.99   | 1.92   | 1.86   | 1.82   | 1.78   | 1.75   |
| 70    | 3.98   | 3.13   | 2.74   | 2.50   | 2.35   | 2.23   | 2.14   | 2.07   | 2.02   | 1.97   | 1.89   | 1.84   | 1.79   | 1.75   | 1.72   |
| 80    | 3.96   | 3.11   | 2.72   | 2.49   | 2.33   | 2.21   | 2.13   | 2.06   | 2.00   | 1.95   | 1.88   | 1.82   | 1.77   | 1.73   | 1.70   |
| 90    | 3.95   | 3.10   | 2.71   | 2.47   | 2.32   | 2.20   | 2.11   | 2.04   | 1.99   | 1.94   | 1.86   | 1.80   | 1.76   | 1.72   | 1.69   |
| 100   | 3.94   | 3.09   | 2.70   | 2.46   | 2.31   | 2.19   | 2.10   | 2.03   | 1.97   | 1.93   | 1.85   | 1.79   | 1.75   | 1.71   | 1.68   |
| 120   | 3.92   | 3.07   | 2.68   | 2.45   | 2.29   | 2.18   | 2.09   | 2.02   | 1.96   | 1.91   | 1.83   | 1.78   | 1.73   | 1.69   | 1.66   |
| 150   | 3.90   | 3.06   | 2.66   | 2.43   | 2.27   | 2.16   | 2.07   | 2.00   | 1.94   | 1.89   | 1.82   | 1.76   | 1.71   | 1.67   | 1.64   |
| 200   | 3.89   | 3.04   | 2.65   | 2.42   | 2.26   | 2.14   | 2.06   | 1.98   | 1.93   | 1.88   | 1.80   | 1.74   | 1.69   | 1.66   | 1.62   |
| 250   | 3.88   | 3.03   | 2.64   | 2.41   | 2.25   | 2.13   | 2.05   | 1.98   | 1.92   | 1.87   | 1.79   | 1.73   | 1.68   | 1.65   | 1.61   |
| 300   | 3.87   | 3.03   | 2.63   | 2.40   | 2.24   | 2.13   | 2.04   | 1.97   | 1.91   | 1.86   | 1.78   | 1.72   | 1.68   | 1.64   | 1.61   |
| 400   | 3.86   | 3.02   | 2.63   | 2.39   | 2.24   | 2.12   | 2.03   | 1.96   | 1.90   | 1.85   | 1.78   | 1.72   | 1.67   | 1.63   | 1.60   |
| 500   | 3.86   | 3.01   | 2.62   | 2.39   | 2.23   | 2.12   | 2.03   | 1.96   | 1.90   | 1.85   | 1.77   | 1.71   | 1.66   | 1.62   | 1.59   |
| 600   | 3.86   | 3.01   | 2.62   | 2.39   | 2.23   | 2.11   | 2.02   | 1.95   | 1.90   | 1.85   | 1.77   | 1.71   | 1.66   | 1.62   | 1.59   |
| 750   | 3.85   | 3.01   | 2.62   | 2.38   | 2.23   | 2.11   | 2.02   | 1.95   | 1.89   | 1.84   | 1.77   | 1.70   | 1.66   | 1.62   | 1.58   |
| 1000  | 3.85   | 3.00   | 2.61   | 2.38   | 2.22   | 2.11   | 2.02   | 1.95   | 1.89   | 1.84   | 1.76   | 1.70   | 1.65   | 1.61   | 1.58   |

TABLE A.3 (continued)

F Distribution: Critical Values of F (5% significance level)

| $v_1$ | 25     | 30     | 35     | 40     | 50     | 60     | 75     | 100    | 150    | 200    |
|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| $v_2$ |        |        |        |        |        |        |        |        |        |        |
| 1     | 249.26 | 250.10 | 250.69 | 251.14 | 251.77 | 252.20 | 252.62 | 253.04 | 253.46 | 253.68 |
| 2     | 19.46  | 19.46  | 19.47  | 19.47  | 19.48  | 19.48  | 19.48  | 19.49  | 19.49  | 19.49  |
| 3     | 8.63   | 8.62   | 8.60   | 8.59   | 8.58   | 8.57   | 8.56   | 8.55   | 8.54   | 8.54   |
| 4     | 5.77   | 5.75   | 5.73   | 5.72   | 5.70   | 5.69   | 5.68   | 5.66   | 5.65   | 5.65   |
| 5     | 4.52   | 4.50   | 4.48   | 4.46   | 4.44   | 4.43   | 4.42   | 4.41   | 4.39   | 4.39   |
| 6     | 3.83   | 3.81   | 3.79   | 3.77   | 3.75   | 3.74   | 3.73   | 3.71   | 3.70   | 3.69   |
| 7     | 3.40   | 3.38   | 3.36   | 3.34   | 3.32   | 3.30   | 3.29   | 3.27   | 3.26   | 3.25   |
| 8     | 3.11   | 3.08   | 3.06   | 3.04   | 3.02   | 3.01   | 2.99   | 2.97   | 2.96   | 2.95   |
| 9     | 2.89   | 2.86   | 2.84   | 2.83   | 2.80   | 2.79   | 2.77   | 2.76   | 2.74   | 2.73   |
| 10    | 2.73   | 2.70   | 2.68   | 2.66   | 2.64   | 2.62   | 2.60   | 2.59   | 2.57   | 2.56   |
| 11    | 2.60   | 2.57   | 2.55   | 2.53   | 2.51   | 2.49   | 2.47   | 2.46   | 2.44   | 2.43   |
| 12    | 2.50   | 2.47   | 2.44   | 2.43   | 2.40   | 2.38   | 2.37   | 2.35   | 2.33   | 2.32   |
| 13    | 2.41   | 2.38   | 2.36   | 2.34   | 2.31   | 2.30   | 2.28   | 2.26   | 2.24   | 2.23   |
| 14    | 2.34   | 2.31   | 2.28   | 2.27   | 2.24   | 2.22   | 2.21   | 2.19   | 2.17   | 2.16   |
| 15    | 2.28   | 2.25   | 2.22   | 2.20   | 2.18   | 2.16   | 2.14   | 2.12   | 2.10   | 2.10   |
| 16    | 2.23   | 2.19   | 2.17   | 2.15   | 2.12   | 2.11   | 2.09   | 2.07   | 2.05   | 2.04   |
| 17    | 2.18   | 2.15   | 2.12   | 2.10   | 2.08   | 2.06   | 2.04   | 2.02   | 2.00   | 1.99   |
| 18    | 2.14   | 2.11   | 2.08   | 2.06   | 2.04   | 2.02   | 2.00   | 1.98   | 1.96   | 1.95   |
| 19    | 2.11   | 2.07   | 2.05   | 2.03   | 2.00   | 1.98   | 1.96   | 1.94   | 1.92   | 1.91   |
| 20    | 2.07   | 2.04   | 2.01   | 1.99   | 1.97   | 1.95   | 1.93   | 1.91   | 1.89   | 1.88   |
| 21    | 2.05   | 2.01   | 1.98   | 1.96   | 1.94   | 1.92   | 1.90   | 1.88   | 1.86   | 1.84   |
| 22    | 2.02   | 1.98   | 1.96   | 1.94   | 1.91   | 1.89   | 1.87   | 1.85   | 1.83   | 1.82   |
| 23    | 2.00   | 1.96   | 1.93   | 1.91   | 1.88   | 1.86   | 1.84   | 1.82   | 1.80   | 1.79   |
| 24    | 1.97   | 1.94   | 1.91   | 1.89   | 1.86   | 1.84   | 1.82   | 1.80   | 1.78   | 1.77   |
| 25    | 1.96   | 1.92   | 1.89   | 1.87   | 1.84   | 1.82   | 1.80   | 1.78   | 1.76   | 1.75   |
| 26    | 1.94   | 1.90   | 1.87   | 1.85   | 1.82   | 1.80   | 1.78   | 1.76   | 1.74   | 1.73   |
| 27    | 1.92   | 1.88   | 1.86   | 1.84   | 1.81   | 1.79   | 1.76   | 1.74   | 1.72   | 1.71   |
| 28    | 1.91   | 1.87   | 1.84   | 1.82   | 1.79   | 1.77   | 1.75   | 1.73   | 1.70   | 1.69   |
| 29    | 1.89   | 1.85   | 1.83   | 1.81   | 1.77   | 1.75   | 1.73   | 1.71   | 1.69   | 1.67   |
| 30    | 1.88   | 1.84   | 1.81   | 1.79   | 1.76   | 1.74   | 1.72   | 1.70   | 1.67   | 1.66   |
| 35    | 1.82   | 1.79   | 1.76   | 1.74   | 1.70   | 1.68   | 1.66   | 1.63   | 1.61   | 1.60   |
| 40    | 1.78   | 1.74   | 1.72   | 1.69   | 1.66   | 1.64   | 1.61   | 1.59   | 1.56   | 1.55   |
| 50    | 1.73   | 1.69   | 1.66   | 1.63   | 1.60   | 1.58   | 1.55   | 1.52   | 1.50   | 1.48   |
| 60    | 1.69   | 1.65   | 1.62   | 1.59   | 1.56   | 1.53   | 1.51   | 1.48   | 1.45   | 1.44   |
| 70    | 1.66   | 1.62   | 1.59   | 1.57   | 1.53   | 1.50   | 1.48   | 1.45   | 1.42   | 1.40   |
| 80    | 1.64   | 1.60   | 1.57   | 1.54   | 1.51   | 1.48   | 1.45   | 1.43   | 1.39   | 1.38   |
| 90    | 1.63   | 1.59   | 1.55   | 1.53   | 1.49   | 1.46   | 1.44   | 1.41   | 1.38   | 1.36   |
| 100   | 1.62   | 1.57   | 1.54   | 1.52   | 1.48   | 1.45   | 1.42   | 1.39   | 1.36   | 1.34   |
| 120   | 1.60   | 1.55   | 1.52   | 1.50   | 1.46   | 1.43   | 1.40   | 1.37   | 1.33   | 1.32   |
| 150   | 1.58   | 1.54   | 1.50   | 1.48   | 1.44   | 1.41   | 1.38   | 1.34   | 1.31   | 1.29   |
| 200   | 1.56   | 1.52   | 1.48   | 1.46   | 1.41   | 1.39   | 1.35   | 1.32   | 1.28   | 1.26   |
| 250   | 1.55   | 1.50   | 1.47   | 1.44   | 1.40   | 1.37   | 1.34   | 1.31   | 1.27   | 1.25   |
| 300   | 1.54   | 1.50   | 1.46   | 1.43   | 1.39   | 1.36   | 1.33   | 1.30   | 1.26   | 1.23   |
| 400   | 1.53   | 1.49   | 1.45   | 1.42   | 1.38   | 1.35   | 1.32   | 1.28   | 1.24   | 1.22   |
| 500   | 1.53   | 1.48   | 1.45   | 1.42   | 1.38   | 1.35   | 1.31   | 1.28   | 1.23   | 1.21   |
| 600   | 1.52   | 1.48   | 1.44   | 1.41   | 1.37   | 1.34   | 1.31   | 1.27   | 1.23   | 1.20   |
| 750   | 1.52   | 1.47   | 1.44   | 1.41   | 1.37   | 1.34   | 1.30   | 1.26   | 1.22   | 1.20   |
| 1000  | 1.52   | 1.47   | 1.43   | 1.41   | 1.36   | 1.33   | 1.30   | 1.26   | 1.22   | 1.19   |

TABLE A.3 (continued)

*F Distribution: Critical Values of F (1% significance level)*

| $v_1$ | 1       | 2       | 3       | 4       | 5       | 6       | 7       | 8       | 9       | 10      | 12      | 14      | 16      | 18      | 20      |
|-------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| $v_2$ |         |         |         |         |         |         |         |         |         |         |         |         |         |         |         |
| 1     | 4052.18 | 4999.50 | 5403.35 | 5624.58 | 5763.65 | 5858.99 | 5928.36 | 5981.07 | 6022.47 | 6055.85 | 6106.32 | 6142.67 | 6170.10 | 6191.53 | 6208.73 |
| 2     | 98.50   | 99.00   | 99.17   | 99.25   | 99.30   | 99.33   | 99.36   | 99.37   | 99.39   | 99.40   | 99.42   | 99.43   | 99.44   | 99.44   | 99.45   |
| 3     | 34.12   | 30.82   | 29.46   | 28.71   | 28.24   | 27.91   | 27.67   | 27.49   | 27.35   | 27.23   | 27.05   | 26.92   | 26.83   | 26.75   | 26.69   |
| 4     | 21.20   | 18.00   | 16.69   | 15.98   | 15.52   | 15.21   | 14.98   | 14.80   | 14.66   | 14.55   | 14.37   | 14.25   | 14.15   | 14.08   | 14.02   |
| 5     | 16.26   | 13.27   | 12.06   | 11.39   | 10.97   | 10.67   | 10.46   | 10.29   | 10.16   | 10.05   | 9.89    | 9.77    | 9.68    | 9.61    | 9.55    |
| 6     | 13.75   | 10.92   | 9.78    | 9.15    | 8.75    | 8.47    | 8.26    | 8.10    | 7.98    | 7.87    | 7.72    | 7.60    | 7.52    | 7.45    | 7.40    |
| 7     | 12.25   | 9.55    | 8.45    | 7.85    | 7.46    | 7.19    | 6.99    | 6.84    | 6.72    | 6.62    | 6.47    | 6.36    | 6.28    | 6.21    | 6.16    |
| 8     | 11.26   | 8.65    | 7.59    | 7.01    | 6.63    | 6.37    | 6.18    | 6.03    | 5.91    | 5.81    | 5.67    | 5.56    | 5.48    | 5.41    | 5.36    |
| 9     | 10.56   | 8.02    | 6.99    | 6.42    | 6.06    | 5.80    | 5.61    | 5.47    | 5.35    | 5.26    | 5.11    | 5.01    | 4.92    | 4.86    | 4.81    |
| 10    | 10.04   | 7.56    | 6.55    | 5.99    | 5.64    | 5.39    | 5.20    | 5.06    | 4.94    | 4.85    | 4.71    | 4.60    | 4.52    | 4.46    | 4.41    |
| 11    | 9.65    | 7.21    | 6.22    | 5.67    | 5.32    | 5.07    | 4.89    | 4.74    | 4.63    | 4.54    | 4.40    | 4.29    | 4.21    | 4.15    | 4.10    |
| 12    | 9.33    | 6.93    | 5.95    | 5.41    | 5.06    | 4.82    | 4.64    | 4.50    | 4.39    | 4.30    | 4.16    | 4.05    | 3.97    | 3.91    | 3.86    |
| 13    | 9.07    | 6.70    | 5.74    | 5.21    | 4.86    | 4.62    | 4.44    | 4.30    | 4.19    | 4.10    | 3.96    | 3.86    | 3.78    | 3.72    | 3.66    |
| 14    | 8.86    | 6.51    | 5.56    | 5.04    | 4.69    | 4.46    | 4.28    | 4.14    | 4.03    | 3.94    | 3.80    | 3.70    | 3.62    | 3.56    | 3.51    |
| 15    | 8.68    | 6.36    | 5.42    | 4.89    | 4.56    | 4.32    | 4.14    | 4.00    | 3.89    | 3.80    | 3.67    | 3.56    | 3.49    | 3.42    | 3.37    |
| 16    | 8.53    | 6.23    | 5.29    | 4.77    | 4.44    | 4.20    | 4.03    | 3.89    | 3.78    | 3.69    | 3.55    | 3.45    | 3.37    | 3.31    | 3.26    |
| 17    | 8.40    | 6.11    | 5.18    | 4.67    | 4.34    | 4.10    | 3.93    | 3.79    | 3.68    | 3.59    | 3.46    | 3.35    | 3.27    | 3.21    | 3.16    |
| 18    | 8.29    | 6.01    | 5.09    | 4.58    | 4.25    | 4.01    | 3.84    | 3.71    | 3.60    | 3.51    | 3.37    | 3.27    | 3.19    | 3.13    | 3.08    |
| 19    | 8.18    | 5.93    | 5.01    | 4.50    | 4.17    | 3.94    | 3.77    | 3.63    | 3.52    | 3.43    | 3.30    | 3.19    | 3.12    | 3.05    | 3.00    |
| 20    | 8.10    | 5.85    | 4.94    | 4.43    | 4.10    | 3.87    | 3.70    | 3.56    | 3.46    | 3.37    | 3.23    | 3.13    | 3.05    | 2.99    | 2.94    |
| 21    | 8.02    | 5.78    | 4.87    | 4.37    | 4.04    | 3.81    | 3.64    | 3.51    | 3.40    | 3.31    | 3.17    | 3.07    | 2.99    | 2.93    | 2.88    |
| 22    | 7.95    | 5.72    | 4.82    | 4.31    | 3.99    | 3.76    | 3.59    | 3.45    | 3.35    | 3.26    | 3.12    | 3.02    | 2.94    | 2.88    | 2.83    |
| 23    | 7.88    | 5.66    | 4.76    | 4.26    | 3.94    | 3.71    | 3.54    | 3.41    | 3.30    | 3.21    | 3.07    | 2.97    | 2.89    | 2.83    | 2.78    |
| 24    | 7.82    | 5.61    | 4.72    | 4.22    | 3.90    | 3.67    | 3.50    | 3.36    | 3.26    | 3.17    | 3.03    | 2.93    | 2.85    | 2.79    | 2.74    |
| 25    | 7.77    | 5.57    | 4.68    | 4.18    | 3.85    | 3.63    | 3.46    | 3.32    | 3.22    | 3.13    | 2.99    | 2.89    | 2.81    | 2.75    | 2.70    |
| 26    | 7.72    | 5.53    | 4.64    | 4.14    | 3.82    | 3.59    | 3.42    | 3.29    | 3.18    | 3.09    | 2.96    | 2.86    | 2.78    | 2.72    | 2.66    |
| 27    | 7.68    | 5.49    | 4.60    | 4.11    | 3.78    | 3.56    | 3.39    | 3.26    | 3.15    | 3.06    | 2.93    | 2.82    | 2.75    | 2.68    | 2.63    |
| 28    | 7.64    | 5.45    | 4.57    | 4.07    | 3.75    | 3.53    | 3.36    | 3.23    | 3.12    | 3.03    | 2.90    | 2.79    | 2.72    | 2.65    | 2.60    |
| 29    | 7.60    | 5.42    | 4.54    | 4.04    | 3.73    | 3.50    | 3.33    | 3.20    | 3.09    | 3.00    | 2.87    | 2.77    | 2.69    | 2.63    | 2.57    |
| 30    | 7.56    | 5.39    | 4.51    | 4.02    | 3.70    | 3.47    | 3.30    | 3.17    | 3.07    | 2.98    | 2.84    | 2.74    | 2.66    | 2.60    | 2.55    |
| 35    | 7.42    | 5.27    | 4.40    | 3.91    | 3.59    | 3.37    | 3.20    | 3.07    | 2.96    | 2.88    | 2.74    | 2.64    | 2.56    | 2.50    | 2.44    |
| 40    | 7.31    | 5.18    | 4.31    | 3.83    | 3.51    | 3.29    | 3.12    | 2.99    | 2.89    | 2.80    | 2.66    | 2.56    | 2.48    | 2.42    | 2.37    |
| 50    | 7.17    | 5.06    | 4.20    | 3.72    | 3.41    | 3.19    | 3.02    | 2.89    | 2.78    | 2.70    | 2.56    | 2.46    | 2.38    | 2.32    | 2.27    |
| 60    | 7.08    | 4.98    | 4.13    | 3.65    | 3.34    | 3.12    | 2.95    | 2.82    | 2.72    | 2.63    | 2.50    | 2.39    | 2.31    | 2.25    | 2.20    |
| 70    | 7.01    | 4.92    | 4.07    | 3.60    | 3.29    | 3.07    | 2.91    | 2.78    | 2.67    | 2.59    | 2.45    | 2.35    | 2.27    | 2.20    | 2.15    |
| 80    | 6.96    | 4.88    | 4.04    | 3.56    | 3.26    | 3.04    | 2.87    | 2.74    | 2.64    | 2.55    | 2.42    | 2.31    | 2.23    | 2.17    | 2.12    |
| 90    | 6.93    | 4.85    | 4.01    | 3.53    | 3.23    | 3.01    | 2.84    | 2.72    | 2.61    | 2.52    | 2.39    | 2.29    | 2.21    | 2.14    | 2.09    |
| 100   | 6.90    | 4.82    | 3.98    | 3.51    | 3.21    | 2.99    | 2.82    | 2.69    | 2.59    | 2.50    | 2.37    | 2.27    | 2.19    | 2.12    | 2.07    |
| 120   | 6.85    | 4.79    | 3.95    | 3.48    | 3.17    | 2.96    | 2.79    | 2.66    | 2.56    | 2.47    | 2.34    | 2.23    | 2.15    | 2.09    | 2.03    |
| 150   | 6.81    | 4.75    | 3.91    | 3.45    | 3.14    | 2.92    | 2.76    | 2.63    | 2.53    | 2.44    | 2.31    | 2.20    | 2.12    | 2.06    | 2.00    |
| 200   | 6.76    | 4.71    | 3.88    | 3.41    | 3.11    | 2.89    | 2.73    | 2.60    | 2.50    | 2.41    | 2.27    | 2.17    | 2.09    | 2.03    | 1.97    |
| 250   | 6.74    | 4.69    | 3.86    | 3.40    | 3.09    | 2.87    | 2.71    | 2.58    | 2.48    | 2.39    | 2.26    | 2.15    | 2.07    | 2.01    | 1.95    |
| 300   | 6.72    | 4.68    | 3.85    | 3.38    | 3.08    | 2.86    | 2.70    | 2.57    | 2.47    | 2.38    | 2.24    | 2.14    | 2.06    | 1.99    | 1.94    |
| 400   | 6.70    | 4.66    | 3.83    | 3.37    | 3.06    | 2.85    | 2.68    | 2.56    | 2.45    | 2.37    | 2.23    | 2.13    | 2.05    | 1.98    | 1.92    |
| 500   | 6.69    | 4.65    | 3.82    | 3.36    | 3.05    | 2.84    | 2.68    | 2.55    | 2.44    | 2.36    | 2.22    | 2.12    | 2.04    | 1.97    | 1.92    |
| 600   | 6.68    | 4.64    | 3.81    | 3.35    | 3.05    | 2.83    | 2.67    | 2.54    | 2.44    | 2.35    | 2.21    | 2.11    | 2.03    | 1.96    | 1.91    |
| 750   | 6.67    | 4.63    | 3.81    | 3.34    | 3.04    | 2.83    | 2.66    | 2.53    | 2.43    | 2.34    | 2.21    | 2.11    | 2.02    | 1.96    | 1.90    |
| 1000  | 6.66    | 4.63    | 3.80    | 3.34    | 3.04    | 2.82    | 2.66    | 2.53    | 2.43    | 2.34    | 2.20    | 2.10    | 2.02    | 1.95    | 1.90    |

## STATISTICAL TABLES

TABLE A.3 (continued)

*F* Distribution: Critical Values of *F* (1% significance level)

| <i>v</i> <sub>1</sub> | 25      | 30      | 35      | 40      | 50      | 60      | 75      | 100     | 150     | 200     |
|-----------------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| <i>v</i> <sub>2</sub> |         |         |         |         |         |         |         |         |         |         |
| 1                     | 6239.83 | 6260.65 | 6275.57 | 6286.78 | 6302.52 | 6313.03 | 6323.56 | 6334.11 | 6344.68 | 6349.97 |
| 2                     | 99.46   | 99.47   | 99.47   | 99.47   | 99.48   | 99.48   | 99.49   | 99.49   | 99.49   | 99.49   |
| 3                     | 26.58   | 26.50   | 26.45   | 26.41   | 26.35   | 26.32   | 26.28   | 26.24   | 26.20   | 26.18   |
| 4                     | 13.91   | 13.84   | 13.79   | 13.75   | 13.69   | 13.65   | 13.61   | 13.58   | 13.54   | 13.52   |
| 5                     | 9.45    | 9.38    | 9.33    | 9.29    | 9.24    | 9.20    | 9.17    | 9.13    | 9.09    | 9.08    |
| 6                     | 7.30    | 7.23    | 7.18    | 7.14    | 7.09    | 7.06    | 7.02    | 6.99    | 6.95    | 6.93    |
| 7                     | 6.06    | 5.99    | 5.94    | 5.91    | 5.86    | 5.82    | 5.79    | 5.75    | 5.72    | 5.70    |
| 8                     | 5.26    | 5.20    | 5.15    | 5.12    | 5.07    | 5.03    | 5.00    | 4.96    | 4.93    | 4.91    |
| 9                     | 4.71    | 4.65    | 4.60    | 4.57    | 4.52    | 4.48    | 4.45    | 4.41    | 4.38    | 4.36    |
| 10                    | 4.31    | 4.25    | 4.20    | 4.17    | 4.12    | 4.08    | 4.05    | 4.01    | 3.98    | 3.96    |
| 11                    | 4.01    | 3.94    | 3.89    | 3.86    | 3.81    | 3.78    | 3.74    | 3.71    | 3.67    | 3.66    |
| 12                    | 3.76    | 3.70    | 3.65    | 3.62    | 3.57    | 3.54    | 3.50    | 3.47    | 3.43    | 3.41    |
| 13                    | 3.57    | 3.51    | 3.46    | 3.43    | 3.38    | 3.34    | 3.31    | 3.27    | 3.24    | 3.22    |
| 14                    | 3.41    | 3.35    | 3.30    | 3.27    | 3.22    | 3.18    | 3.15    | 3.11    | 3.08    | 3.06    |
| 15                    | 3.28    | 3.21    | 3.17    | 3.13    | 3.08    | 3.05    | 3.01    | 2.98    | 2.94    | 2.92    |
| 16                    | 3.16    | 3.10    | 3.05    | 3.02    | 2.97    | 2.93    | 2.90    | 2.86    | 2.83    | 2.81    |
| 17                    | 3.07    | 3.00    | 2.96    | 2.92    | 2.87    | 2.83    | 2.80    | 2.76    | 2.73    | 2.71    |
| 18                    | 2.98    | 2.92    | 2.87    | 2.84    | 2.78    | 2.75    | 2.71    | 2.68    | 2.64    | 2.62    |
| 19                    | 2.91    | 2.84    | 2.80    | 2.76    | 2.71    | 2.67    | 2.64    | 2.60    | 2.57    | 2.55    |
| 20                    | 2.84    | 2.78    | 2.73    | 2.69    | 2.64    | 2.61    | 2.57    | 2.54    | 2.50    | 2.48    |
| 21                    | 2.79    | 2.72    | 2.67    | 2.64    | 2.58    | 2.55    | 2.51    | 2.48    | 2.44    | 2.42    |
| 22                    | 2.73    | 2.67    | 2.62    | 2.58    | 2.53    | 2.50    | 2.46    | 2.42    | 2.38    | 2.36    |
| 23                    | 2.69    | 2.62    | 2.57    | 2.54    | 2.48    | 2.45    | 2.41    | 2.37    | 2.34    | 2.32    |
| 24                    | 2.64    | 2.58    | 2.53    | 2.49    | 2.44    | 2.40    | 2.37    | 2.33    | 2.29    | 2.27    |
| 25                    | 2.60    | 2.54    | 2.49    | 2.45    | 2.40    | 2.36    | 2.33    | 2.29    | 2.25    | 2.23    |
| 26                    | 2.57    | 2.50    | 2.45    | 2.42    | 2.36    | 2.33    | 2.29    | 2.25    | 2.21    | 2.19    |
| 27                    | 2.54    | 2.47    | 2.42    | 2.38    | 2.33    | 2.29    | 2.26    | 2.22    | 2.18    | 2.16    |
| 28                    | 2.51    | 2.44    | 2.39    | 2.35    | 2.30    | 2.26    | 2.23    | 2.19    | 2.15    | 2.13    |
| 29                    | 2.48    | 2.41    | 2.36    | 2.33    | 2.27    | 2.23    | 2.20    | 2.16    | 2.12    | 2.10    |
| 30                    | 2.45    | 2.39    | 2.34    | 2.30    | 2.25    | 2.21    | 2.17    | 2.13    | 2.09    | 2.07    |
| 35                    | 2.35    | 2.28    | 2.23    | 2.19    | 2.14    | 2.10    | 2.06    | 2.02    | 1.98    | 1.96    |
| 40                    | 2.27    | 2.20    | 2.15    | 2.11    | 2.06    | 2.02    | 1.98    | 1.94    | 1.90    | 1.87    |
| 50                    | 2.17    | 2.10    | 2.05    | 2.01    | 1.95    | 1.91    | 1.87    | 1.82    | 1.78    | 1.76    |
| 60                    | 2.10    | 2.03    | 1.98    | 1.94    | 1.88    | 1.84    | 1.79    | 1.75    | 1.70    | 1.68    |
| 70                    | 2.05    | 1.98    | 1.93    | 1.89    | 1.83    | 1.78    | 1.74    | 1.70    | 1.65    | 1.62    |
| 80                    | 2.01    | 1.94    | 1.89    | 1.85    | 1.79    | 1.75    | 1.70    | 1.65    | 1.61    | 1.58    |
| 90                    | 1.99    | 1.92    | 1.86    | 1.82    | 1.76    | 1.72    | 1.67    | 1.62    | 1.57    | 1.55    |
| 100                   | 1.97    | 1.89    | 1.84    | 1.80    | 1.74    | 1.69    | 1.65    | 1.60    | 1.55    | 1.52    |
| 120                   | 1.93    | 1.86    | 1.81    | 1.76    | 1.70    | 1.66    | 1.61    | 1.56    | 1.51    | 1.48    |
| 150                   | 1.90    | 1.83    | 1.77    | 1.73    | 1.66    | 1.62    | 1.57    | 1.52    | 1.46    | 1.43    |
| 200                   | 1.87    | 1.79    | 1.74    | 1.69    | 1.63    | 1.58    | 1.53    | 1.48    | 1.42    | 1.39    |
| 250                   | 1.85    | 1.77    | 1.72    | 1.67    | 1.61    | 1.56    | 1.51    | 1.46    | 1.40    | 1.36    |
| 300                   | 1.84    | 1.76    | 1.70    | 1.66    | 1.59    | 1.55    | 1.50    | 1.44    | 1.38    | 1.35    |
| 400                   | 1.82    | 1.75    | 1.69    | 1.64    | 1.58    | 1.53    | 1.48    | 1.42    | 1.36    | 1.32    |
| 500                   | 1.81    | 1.74    | 1.68    | 1.63    | 1.57    | 1.52    | 1.47    | 1.41    | 1.34    | 1.31    |
| 600                   | 1.80    | 1.73    | 1.67    | 1.63    | 1.56    | 1.51    | 1.46    | 1.40    | 1.34    | 1.30    |
| 750                   | 1.80    | 1.72    | 1.66    | 1.62    | 1.55    | 1.50    | 1.45    | 1.39    | 1.33    | 1.29    |
| 1000                  | 1.79    | 1.72    | 1.66    | 1.61    | 1.54    | 1.50    | 1.44    | 1.38    | 1.32    | 1.28    |