### DEPARTMENT OF STATISTICS AND DEMOGRAPHY

### MAIN EXAMINATION, 2011/12

**COURSE TITLE:** 

# **OPERATIONS RESEARCH I**

**COURSE CODE:** 

ST 307

TIME ALLOWED:

**TWO (2) HOURS** 

**INSTRUCTION:** 

ANSWER QUESTION <u>ONE</u> AND <u>ANY TWO</u> QUESTIONS ALL QUESTIONS CARRY EQUAL MARKS AS GIVEN IN PARENTHESIS

SPECIAL REQUIREMENTS:

SCIENTIFIC CALCULATORS AND GRAPH PAPER

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### Question 1

Consider the following linear programming problem Maximise  $Z = 2x_1 + 3x_2$ Subject to

 $x_1 + 2x_2 \le 10$   $3x_1 + x_2 \le 15$   $x_2 \le 4$  $x_1, x_2 \ge 0$ 

(a) Solve this problem using the graphical method

(b) Find the range of values for the objective function coefficients for which the current optimal solution will remain optimal.

(c) Which resource is to be given top priority when the allocation of resources is made and why?

(20 marks)

### **Question 2**

(a) Briefly define the following terms as used in linear programming

(i) Infeasible solution

(ii) Degeneracy

(iii) Alternative optimal solution

(b) (i) Solve the following linear program using the simplex method.

Maximize  $Z = 3x_1 + 2x_2 + 5x_3$ Subject to

 $x_{1} + 2x_{2} + x_{3} \le 430$  $3x_{1} + 2x_{3} \le 460$  $x_{1} + 4x_{2} \le 420$  $x_{1}, x_{2}, x_{3} \ge 0$ 

(ii) Identify shadow prices for the resources and explain their significance.

(20 marks)

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# Question 3

Given the following primal problem Minimize  $Z = 10x_1 + 5x_2 + 4x_3$ 

Subject to

 $3x_1 + 2x_2 - 3x_3 \ge 3$   $4x_1 + 2x_3 \ge 10$  $x_1, x_2, x_3 \ge 0$ 

(a) Obtain the dual for this problem.

(b) Solve the dual problem using the simplex method.

(c) Use the dual solution to identify the optimal solution to the original primal problem.

(20 marks)

#### **Question 4**

A product is produced at three plants and shipped to three warehouses. The transportation costs per unit are shown in the following table:

	Warehouse			
Plant	W1	W2	W3	Plant Capacity/Supply
P1	20	16	24	300
P2	10	10	8	500
Р3	12	18	10	100
Warehouse demand	200	400	300	

(a) Use the Northwest corner rule method to find the initial basic feasible solution

(b) Find the optimal solution to this problem.

(c) Express the transportation problem as a linear programming problem.

(20 marks)

#### **Question 5**

Swazi Auto Spares wants to advertise his products on national radio or television (TV). The advertisement budget is limited to E10,000 a month. Each minute of radio advertisement costs E15 and each minute of TV commercials cost E300. The shop likes to use radio advertisement at least twice as much as TV. In the meantime it is not practical to use more than 400 minutes of radio advertisement per month. Past experience shows that TV advertisement is estimated to be 25 times more effective than that of radio. Determine the optimal allocation of the budget to radio and TV advertisements.

(20 marks)

#### END OF EXAM!!